

Compute the following integrals using either u -substitution or integration by parts.

1. $\int \frac{\ln x}{x^{3/2}} dx$

$u = \ln x, dv = x^{-3/2}$, this yields

$$-2x^{-1/2} \ln x - \int (-x^{-1/2}) \frac{1}{x} dx = -\frac{2 \ln x}{\sqrt{x}} + \int x^{-3/2} dx = -\frac{2 \ln x}{\sqrt{x}} - \frac{2}{\sqrt{x}} + C$$

2. $\int \arctan x dx$

$u = \arctan x, dv = dx$ this yields

$$x \arctan x - \int \frac{x}{1+x^2} dx = x \arctan x - \frac{1}{2} \ln(1+x^2) + C.$$

3. $\int \arcsin(x) dx$

$u = \arcsin x, dv = dx$ this yields

$$x \arcsin x - \int \frac{x}{\sqrt{1-x^2}} dx = x \arcsin x + \sqrt{1-x^2} + C$$

4. $\int e^x \ln(1+e^x) \sqrt{1+e^x} dx$

First make substitution $t = 1 + e^x$. This gives

$$\int \ln(t) \sqrt{t} dt$$

Now let $u = \ln t, dv = \sqrt{t}$, this yields

$$\frac{2}{3} t^{3/2} \ln t - \frac{2}{3} \int t^{3/2} \frac{1}{t} dt = \frac{2}{3} t^{3/2} \ln t - \frac{4}{9} t^{3/2} + C$$

Now change back to $t = 1 + e^x$

$$\frac{2}{3} (1+e^x)^{3/2} \ln(1+e^x) - \frac{4}{9} (1+e^x)^{3/2} + C$$

5. $\int x^2 e^{\frac{x}{2}} dx$. Do integration by parts twice and be careful. Should get some variant of

$$2e^{x/2}(x^2 - 4x + 8) + C$$