

# LAKSHYA BATCH



JEE

**MAGNETISM AND MATTER**  
**GAUSS LAW AND EARTH MAGNETISM**

**LECTURE - 5**



# GOALS OF THE DAY



1

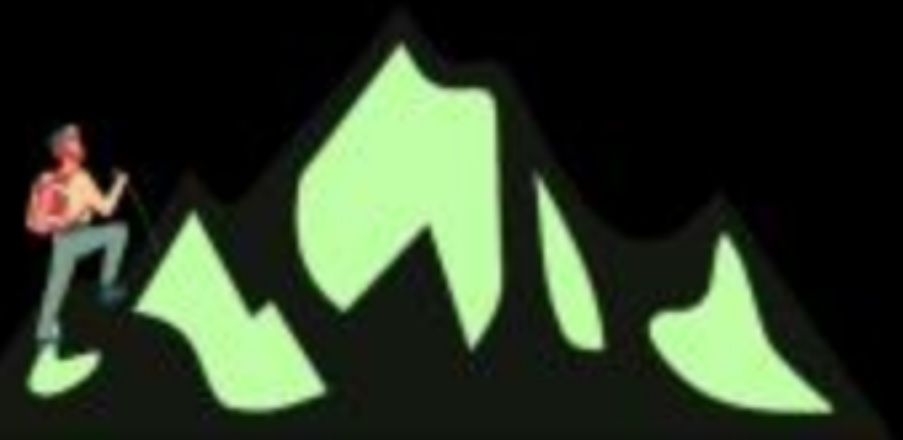
GAUSS'S LAW,

2

EARTH'S MAGNETISM

3

RELATION BETWEEN HORIZONTAL COMPONENT,  
VERTICAL COMPONENT AND ANGLE OF DIP



# Gauss law of Magnetostatics (Not in Boards).

$$\oint \vec{B} \cdot d\vec{A} = \mu_0 (m_{in})$$

$m$  = Pole Strength.

We do not have monopoles.

$$= \mu_0 (+m - m)$$

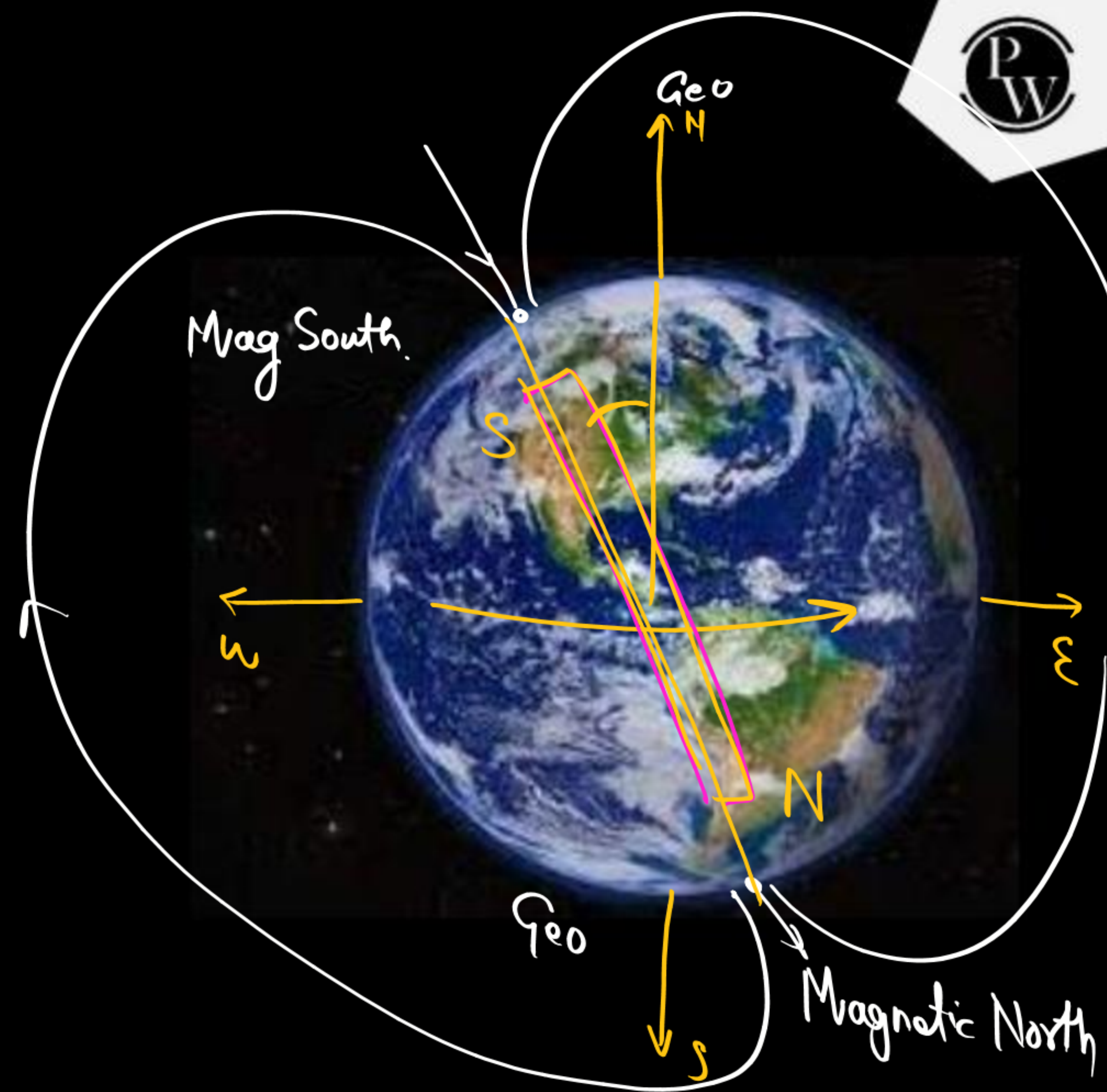
$$\oint \vec{B} \cdot d\vec{A} = 0$$

Magnetic flux through a closed surface is always zero.

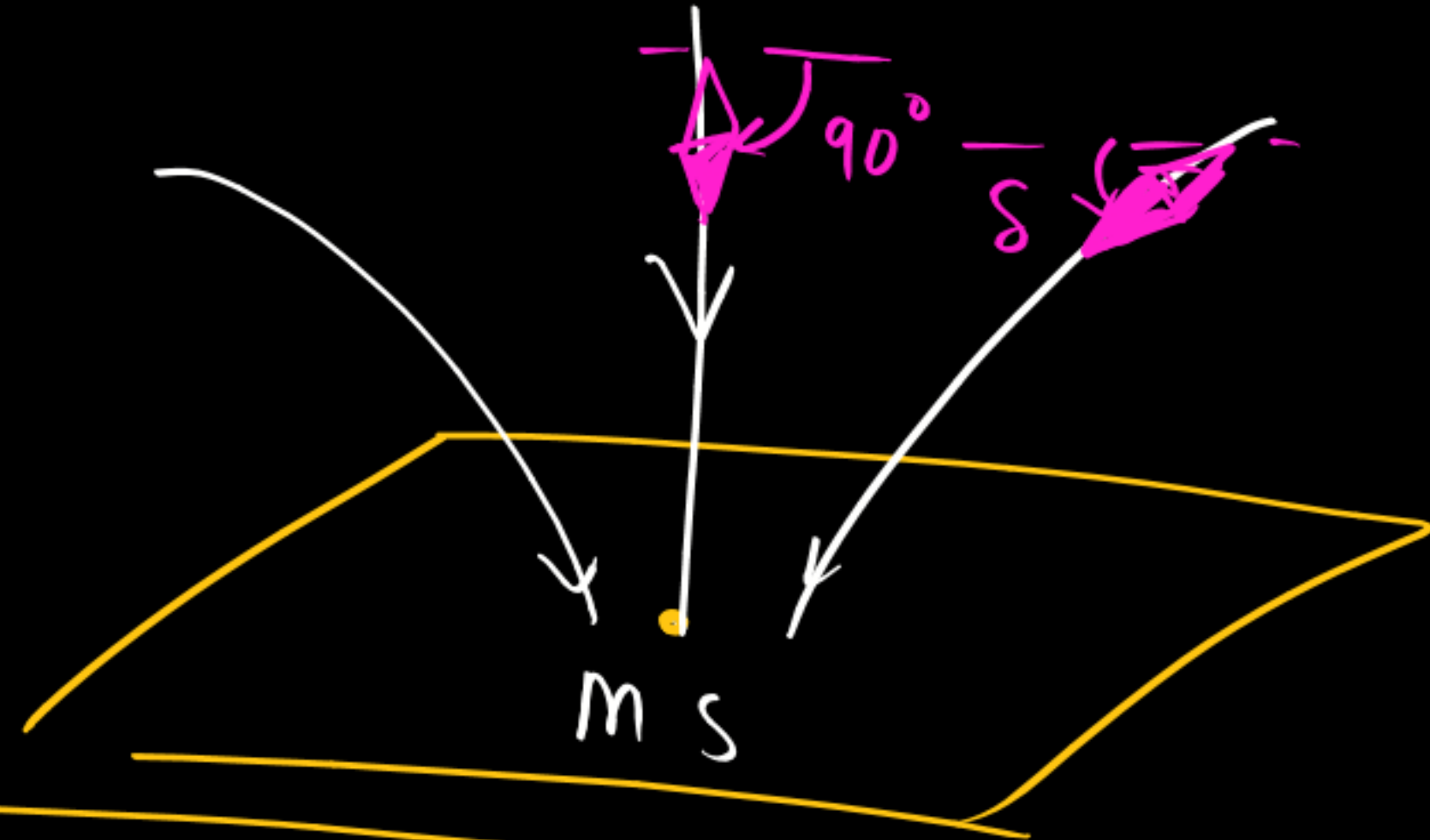
# EARTH'S MAGNETISM



Reason:- hypothesis.  
due to Rotating Molten  
Core (free Ions) we  
assume there is some  
Current Inside Core due to  
which there is Earth Magnetic  
field.



Exactly at Poles



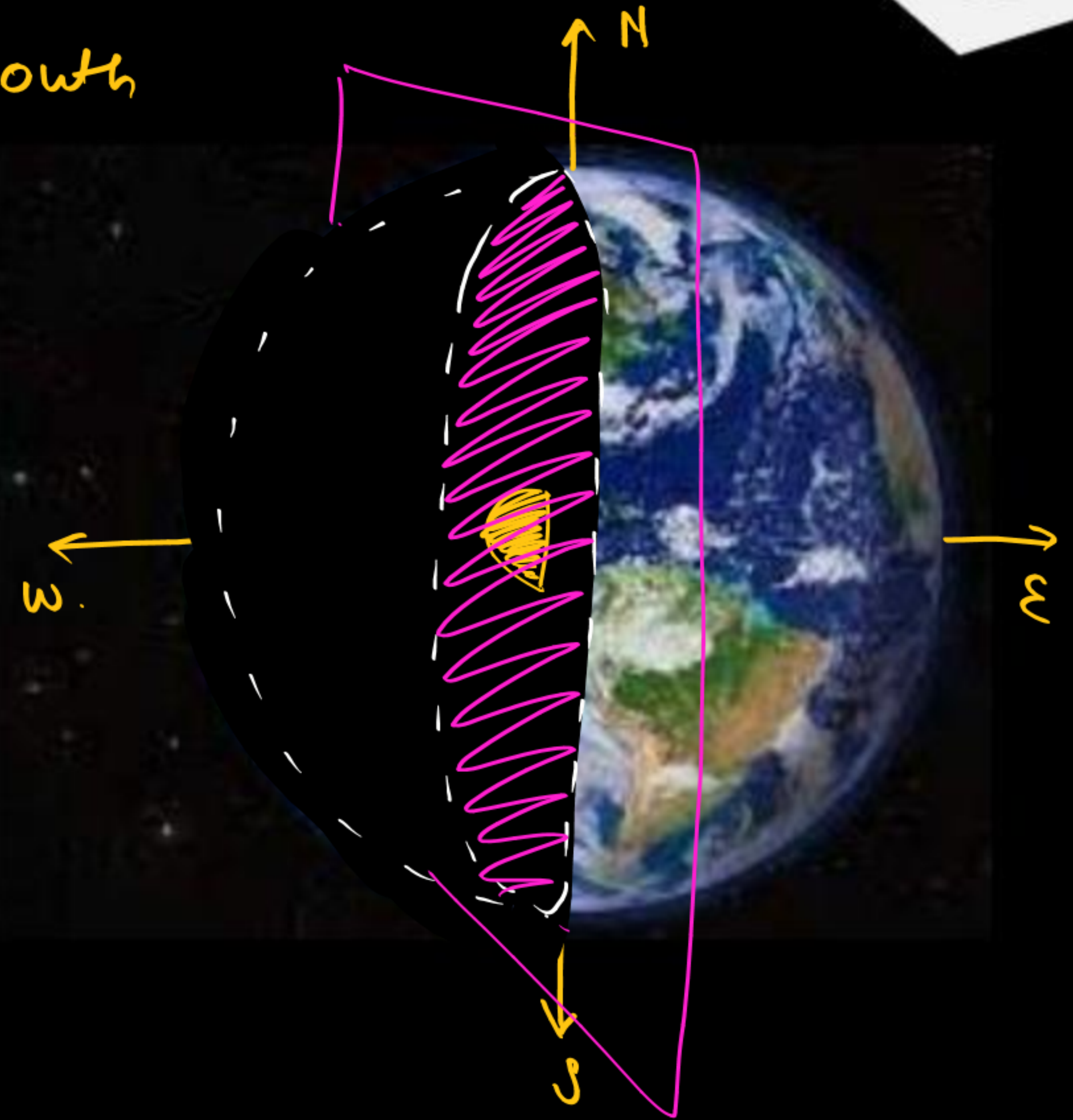
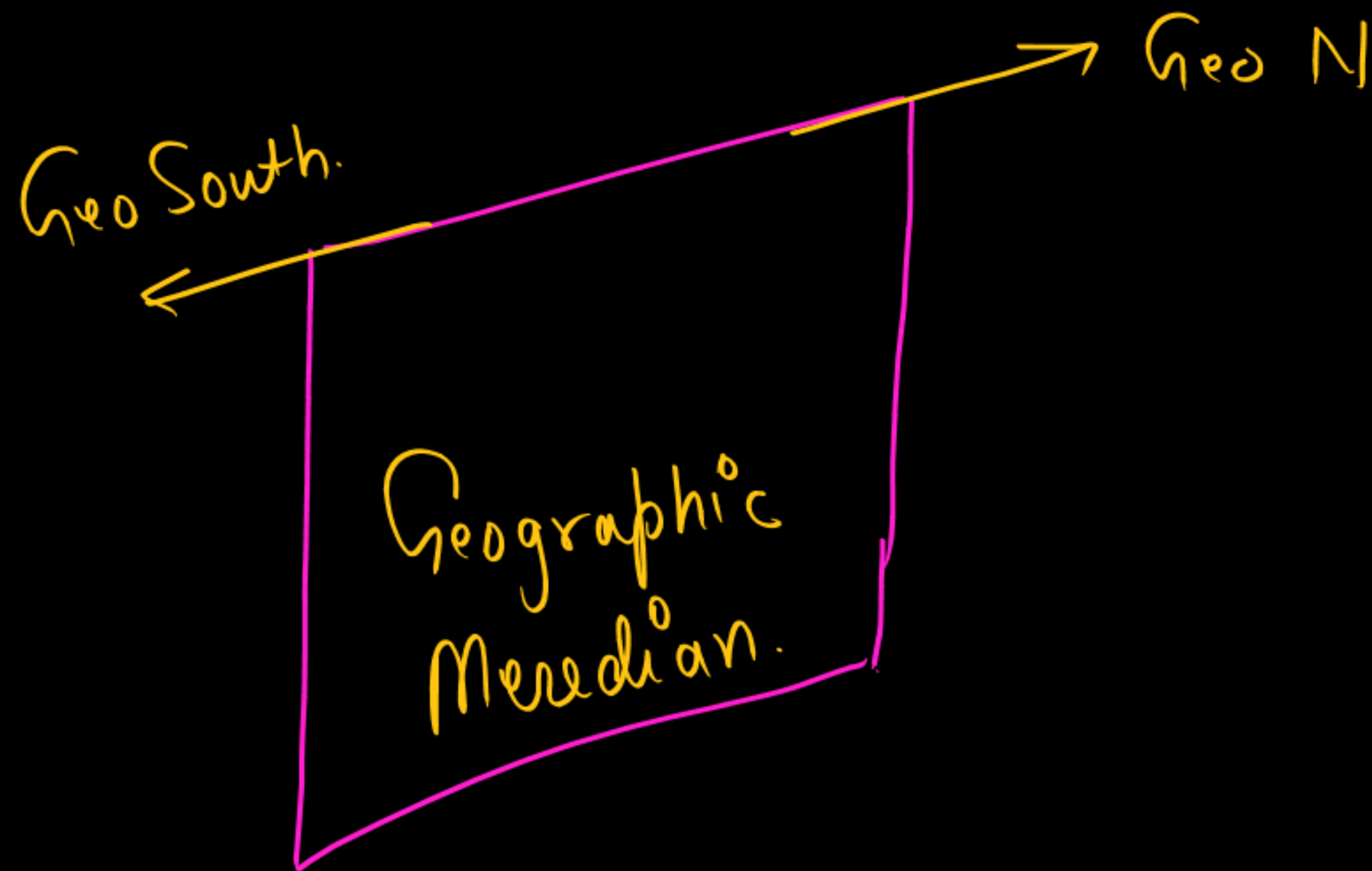
$\angle$  Magnetic Poles =  $90^\circ$   
 $\angle$  Equator =  $0^\circ$



$\angle$  of inclination =  $90^\circ$

# Geographic Meridian.

The plane which include Geo N & Geo South is called Geographic Meridian.

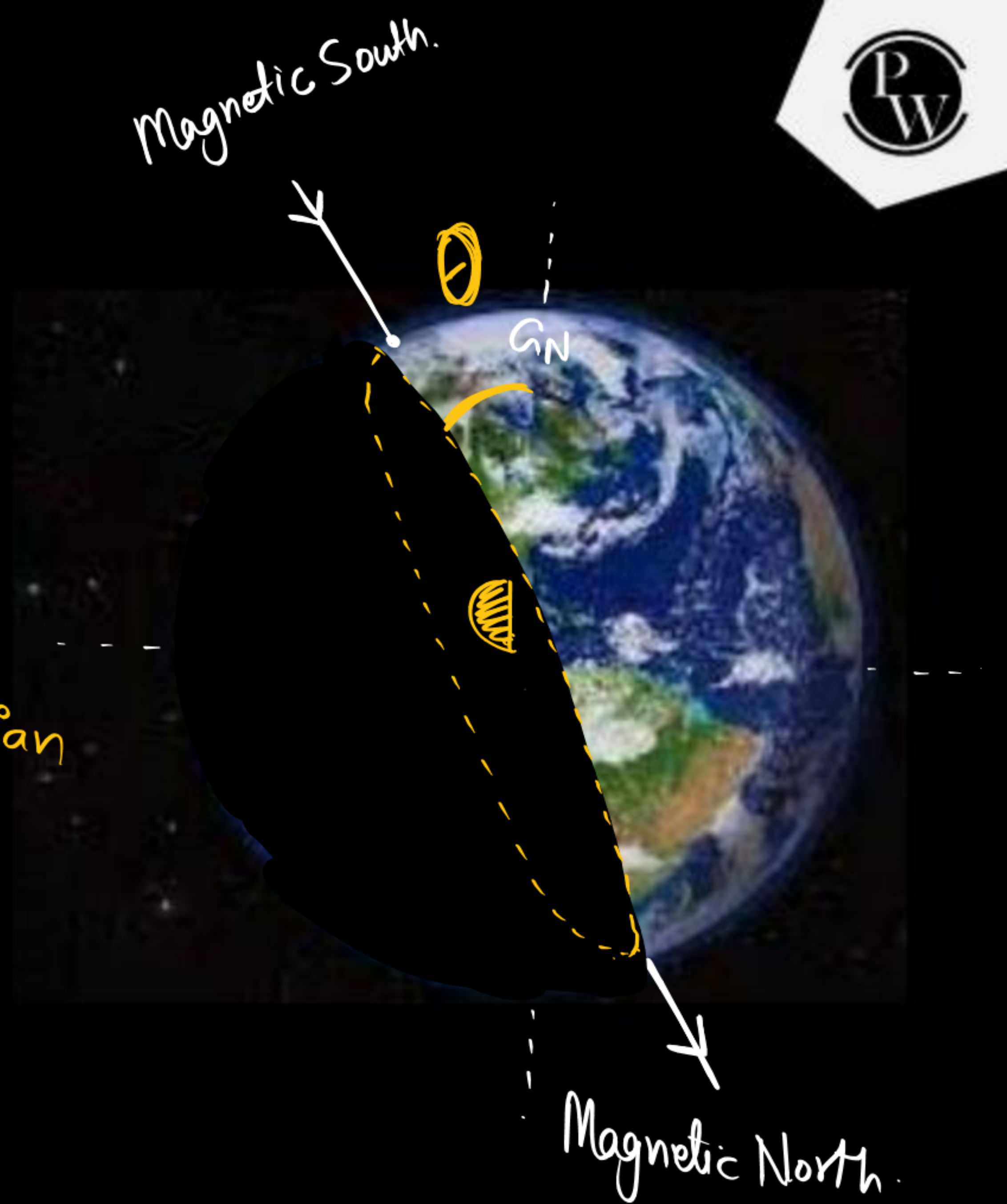


# Magnetic Meridian

Plane passing through Magnetic South & North Pole is called Magnetic Meridian.

$\theta$  = Angle between Geographic Meridian & Magnetic Meridian.

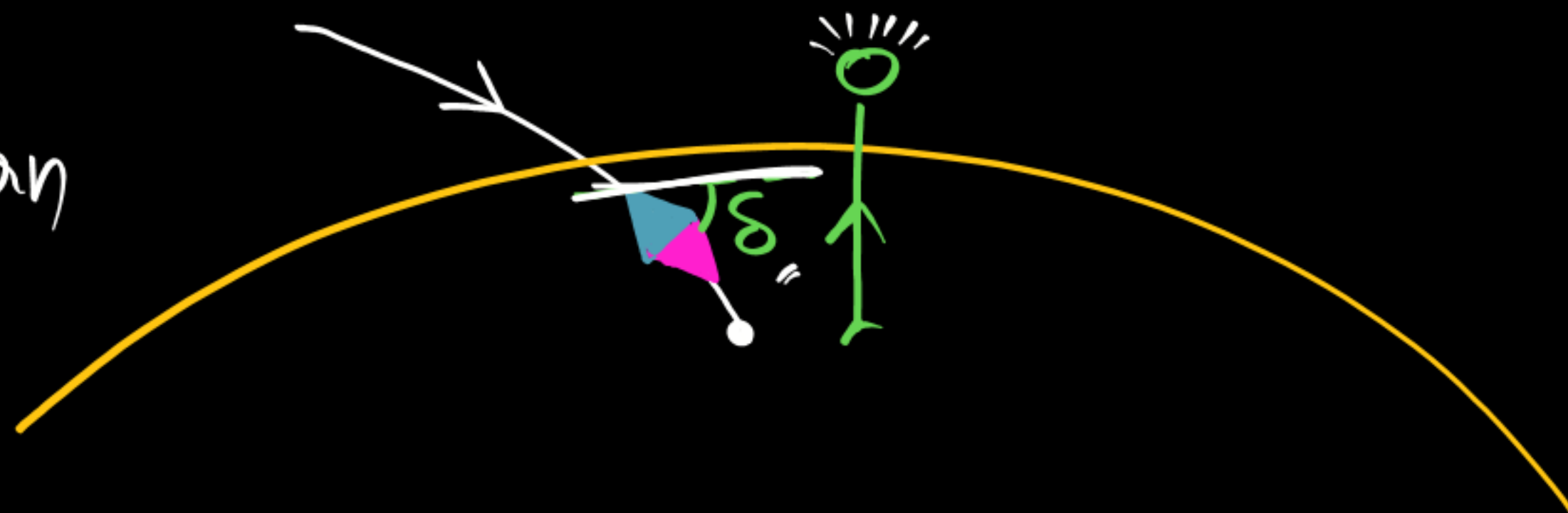
Angle of declination  
 $\theta_{\text{Earth}} \approx 11^\circ$



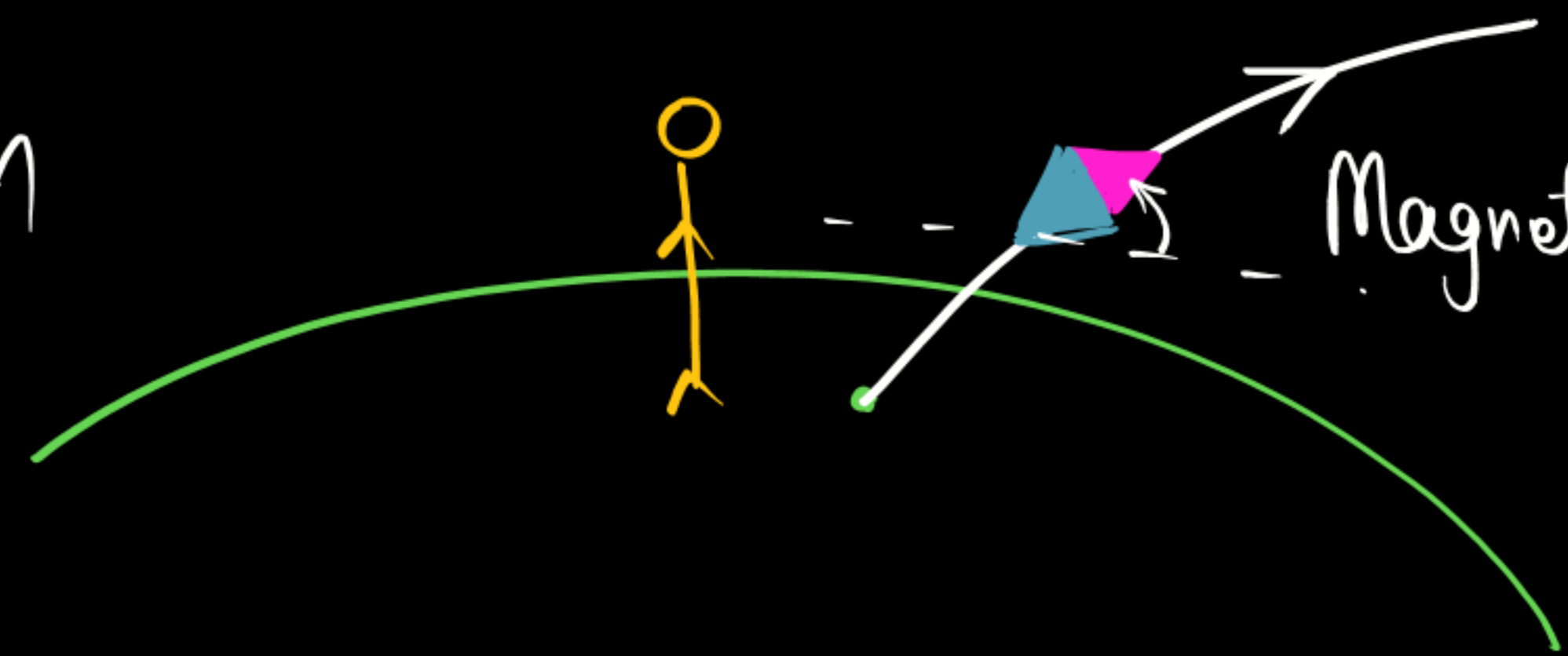
Magnetic dip angle

Magnetic inclination (dip)

Northern hemi

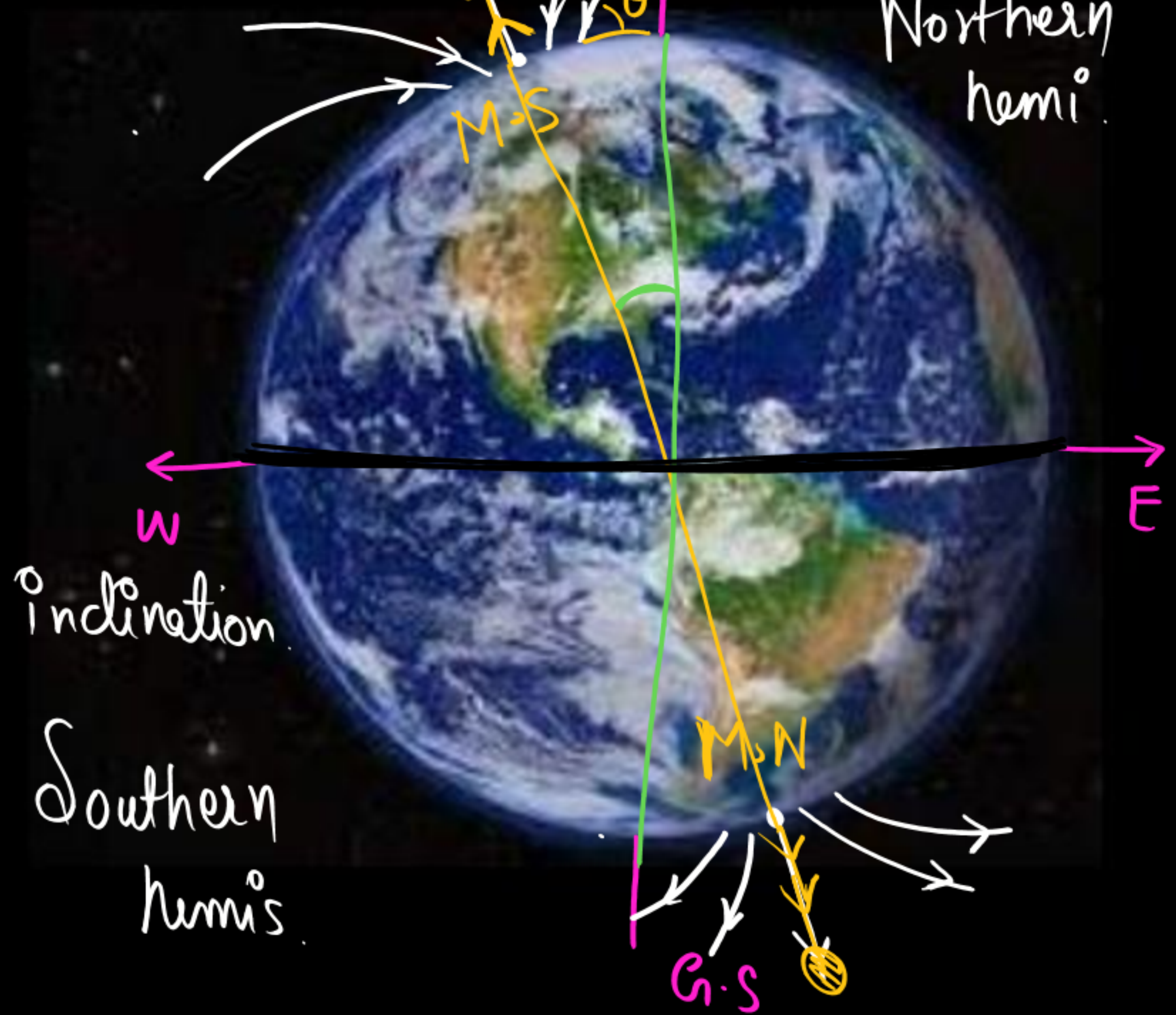


Southern hemi



Magnetic inclination

Southern hemis



Northern hemi



## Three components of earth Magnetic Field:

1. Magnetic Declination ( $\theta$ )

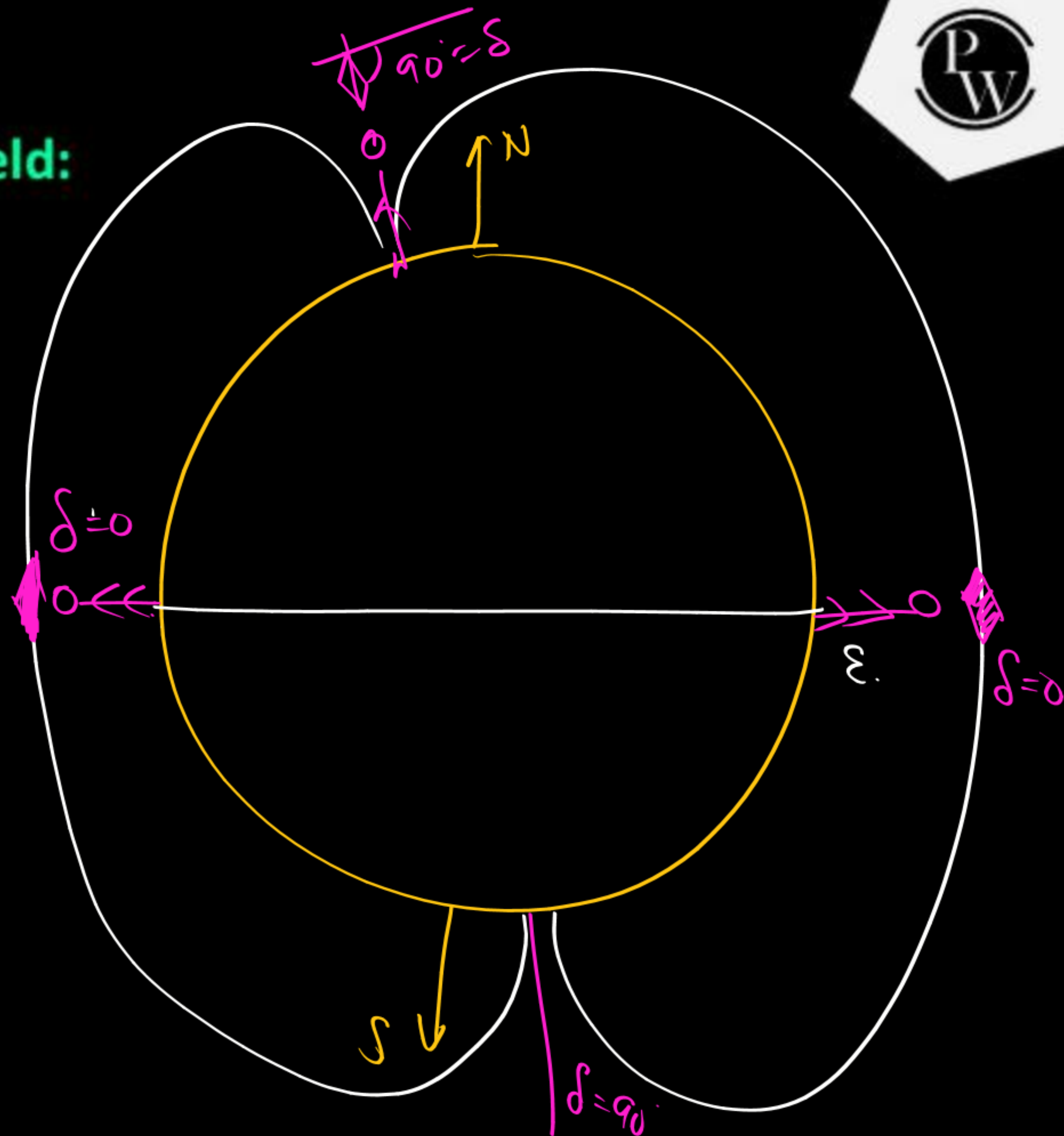


2. Magnetic inclination (Dip)

(Southern hemi) (Northern hemi)



3. Horizontal component



Three components of earth Magnetic Field:

**Magnetic Declination :**

The  $\angle$  between Geographic Meridian & Magnetic Meridian.

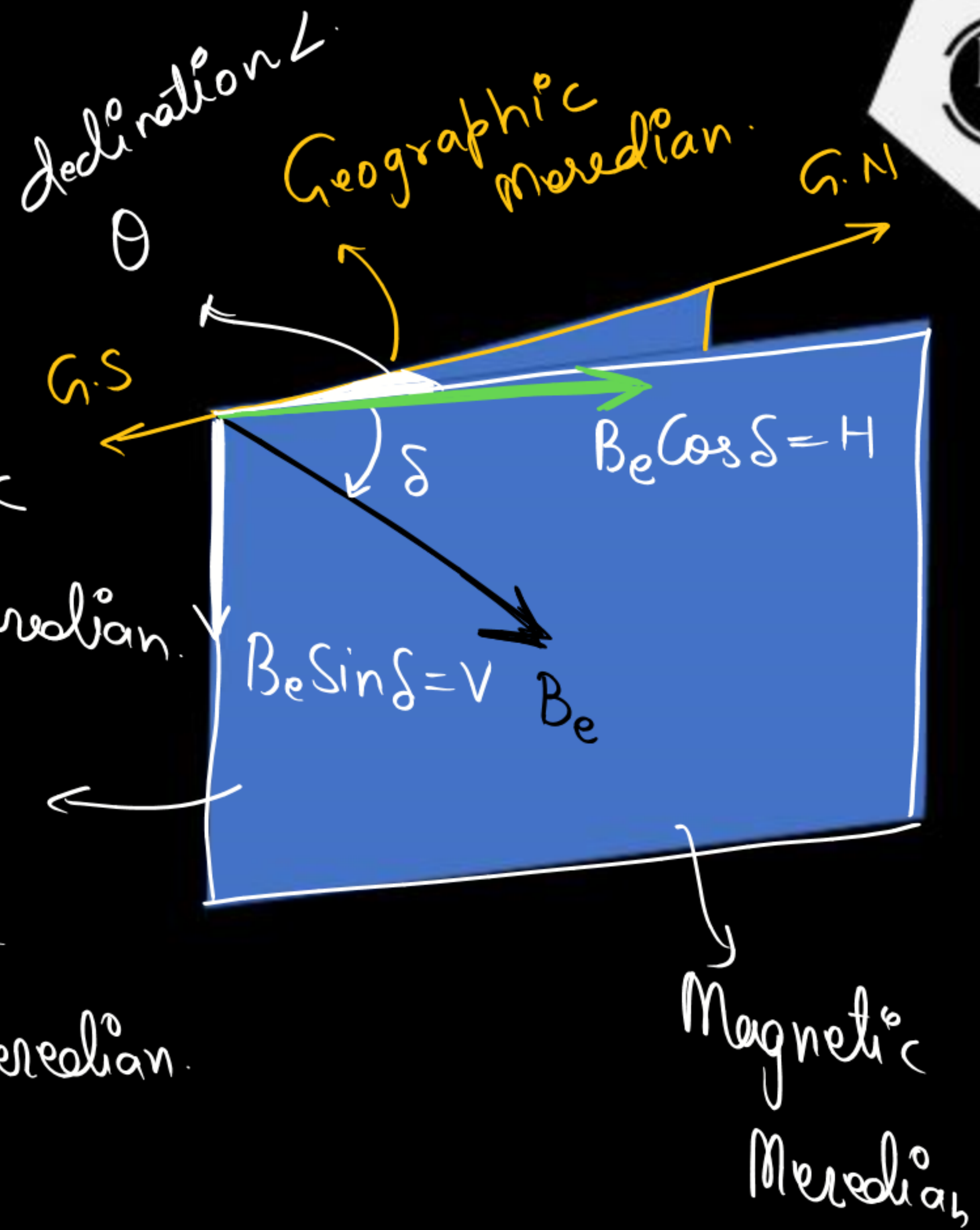


Three components of earth Magnetic Field:

**Magnetic inclination (Dip) :**

The angle made by Earth Magnetic field with horizontal in Magnetic Meridian.

Earth Magnetic field will be Magnetic Meridian.



Three components of earth Magnetic Field:

Horizontal component

The Component of Earth Magnetic field in horizontal dir  
is called Horizontal Component.



- **Isogonic Lines**: The lines on map joining same magnetic declination
- **Aganoic**: the lines which passes through places having zero declination
- **Isoclinic Lines**: These are the lines joining same dip
- **Aclinic Lines**: The lines joining places of zero dip
- **Isodynamic Lines**: The lines Joining the places having same horizontal earth Component



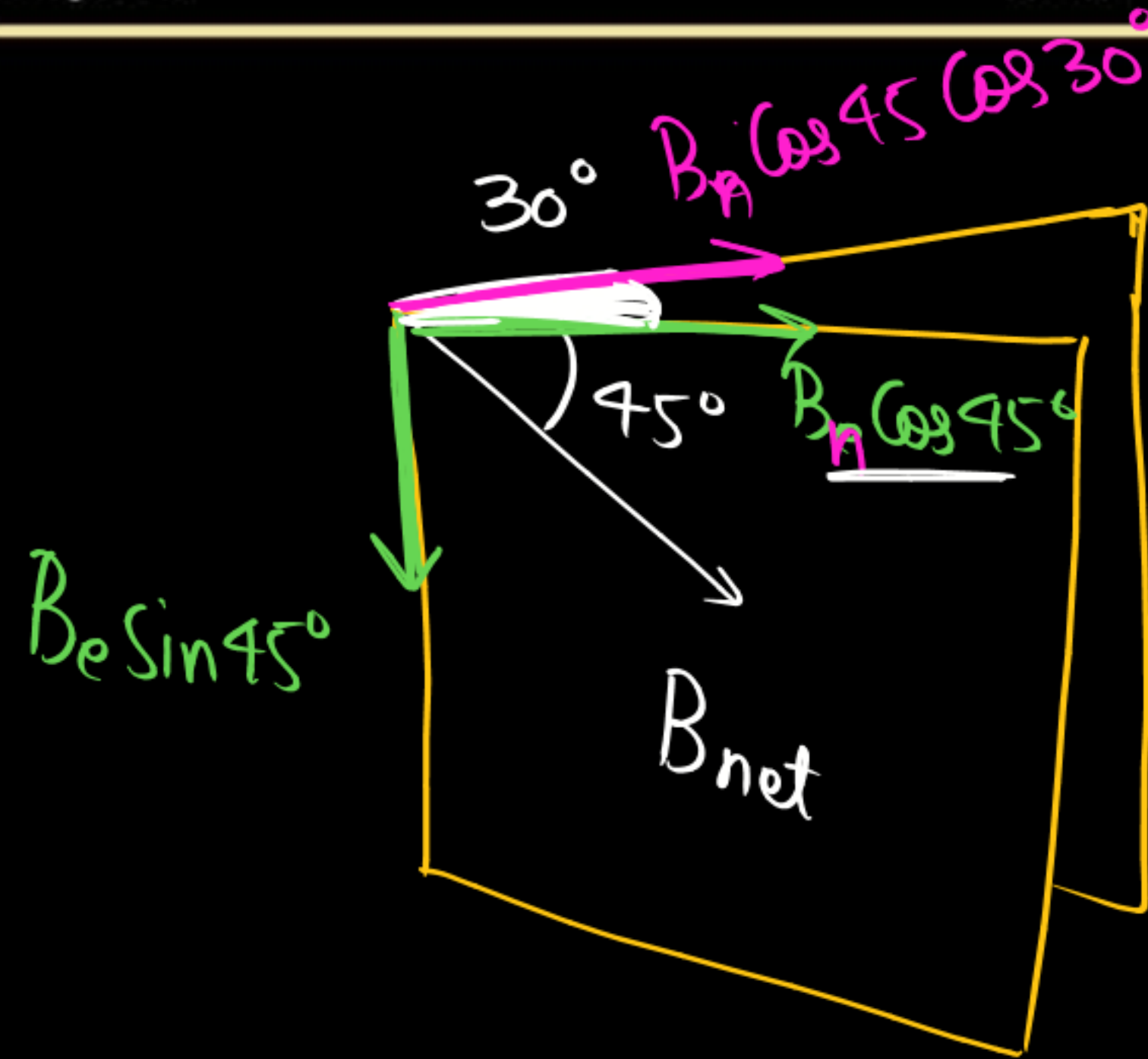
If a magnet is suspended at an angle  $30^\circ$  to the magnetic meridian, it makes an angle of  $45^\circ$  with the horizontal. The real dip is

(a)  $\tan^{-1}(\sqrt{3}/2)$

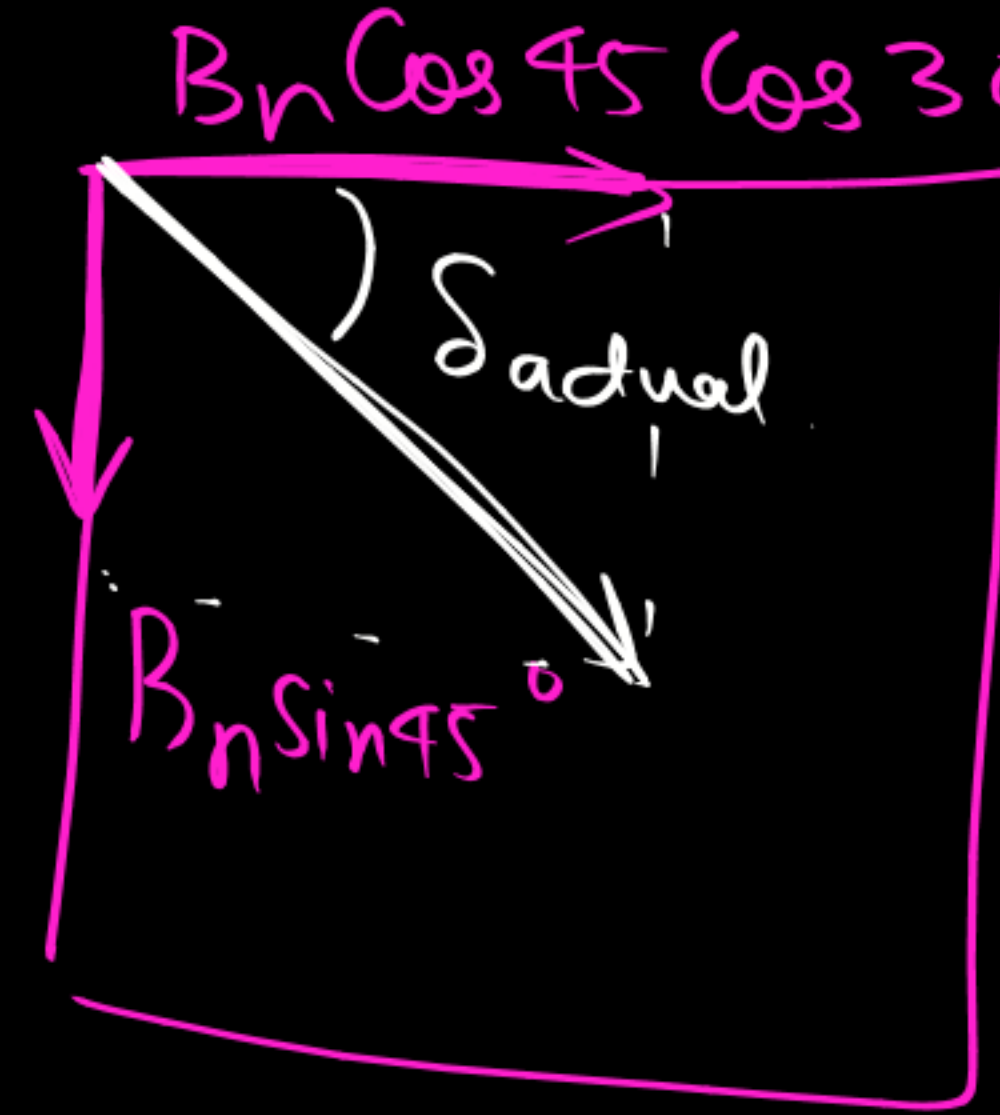
(b)  $\tan^{-1}(\sqrt{3})$

(c)  $\tan^{-1}(\sqrt{3}/2)$

(d)  $\tan^{-1}(2/\sqrt{3})$  Ans



Magnetic Meridian. (Real dip will be in Magnetic Meridian).



$$\tan \delta = \frac{P}{B} = \frac{B_n \sin 45}{B_n \cos 45 \cos 30} = \frac{2}{\sqrt{3}}$$

$$\delta_{real} = \tan^{-1}\left(\frac{2}{\sqrt{3}}\right)$$



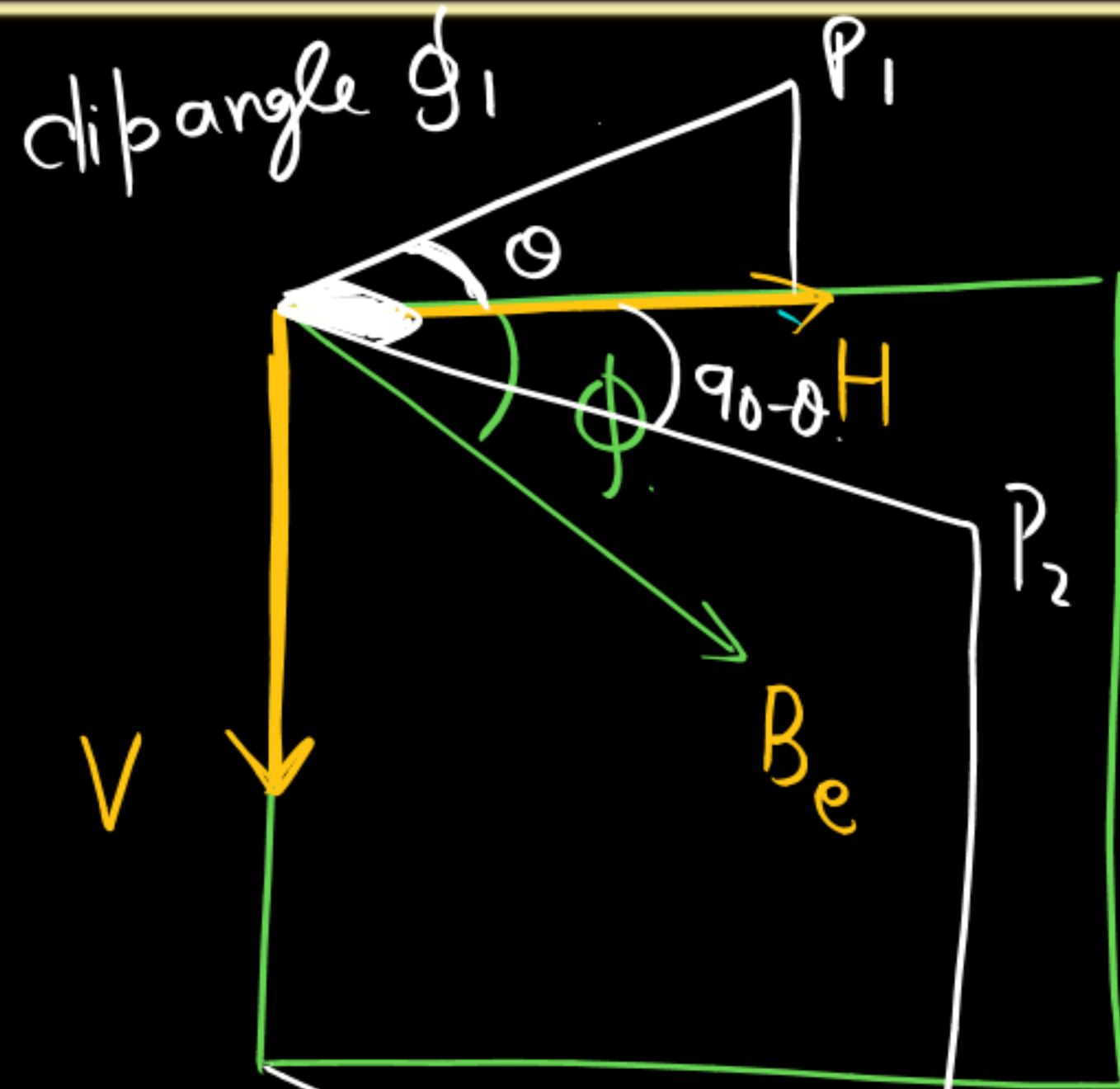
If  $\phi_1$  and  $\phi_2$  be the angles of dip observed in two vertical planes at right angles to each other and  $\phi$  be the true angle of dip, then (PYQ)

(a)  $\cos^2 \phi = \cos^2 \phi_1 + \cos^2 \phi_2$

(b)  $\sec^2 \phi = \sec^2 \phi_1 + \sec^2 \phi_2$

(c)  $\tan^2 \phi = \tan^2 \phi_1 + \tan^2 \phi_2$

(d)  $\cot^2 \phi = \cot^2 \phi_1 + \cot^2 \phi_2$



Magnetic Meridian

$P_1$  &  $P_2$  are at  $90^\circ$  to Each other

$\tan \phi_1 = \frac{\tan \phi}{\cos \theta}$

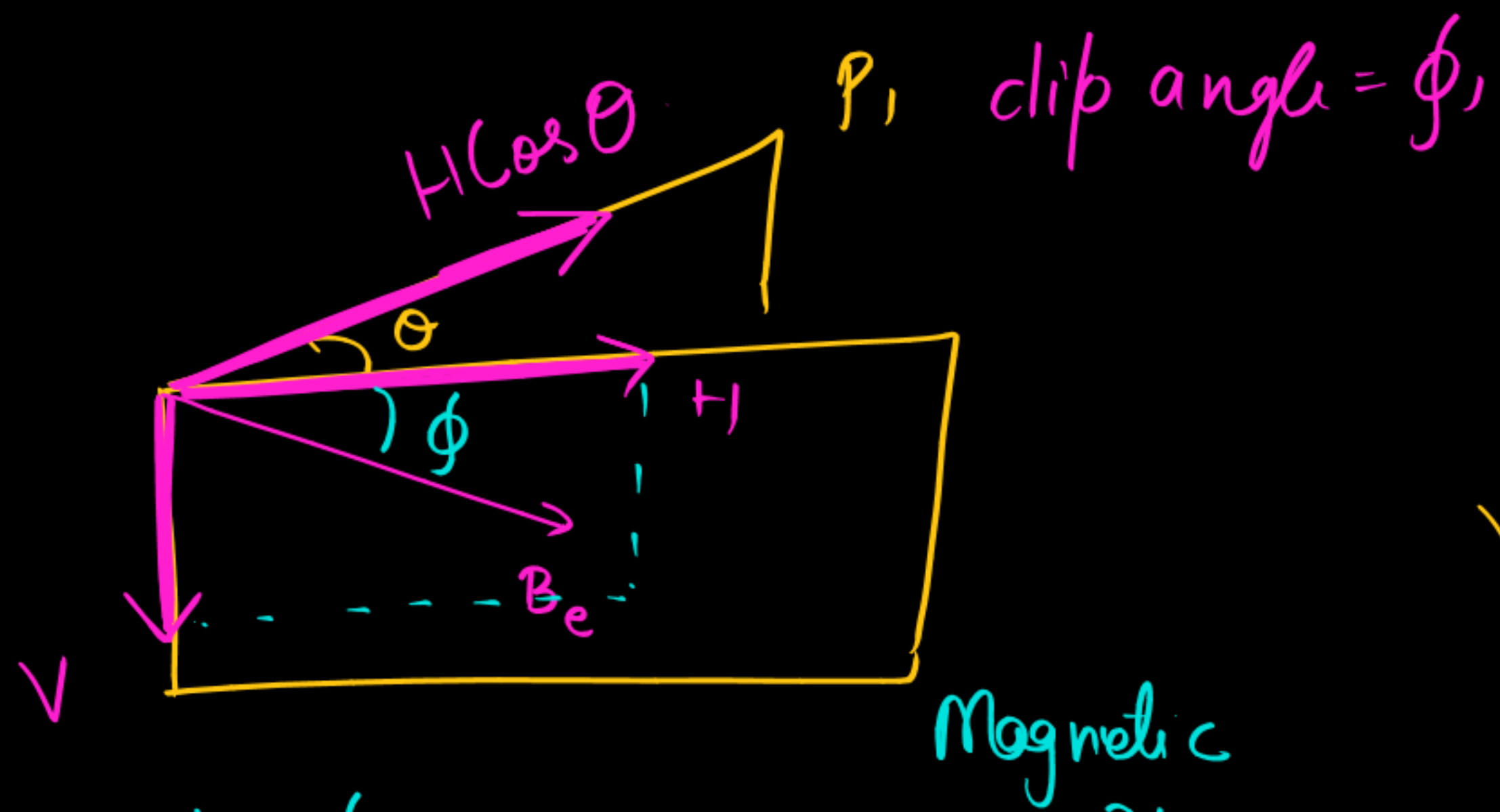
Other  $\tan \phi_2 = \frac{\tan \phi}{\sin \theta}$

$\cos \theta = \frac{\tan \phi}{\tan \phi_1}$

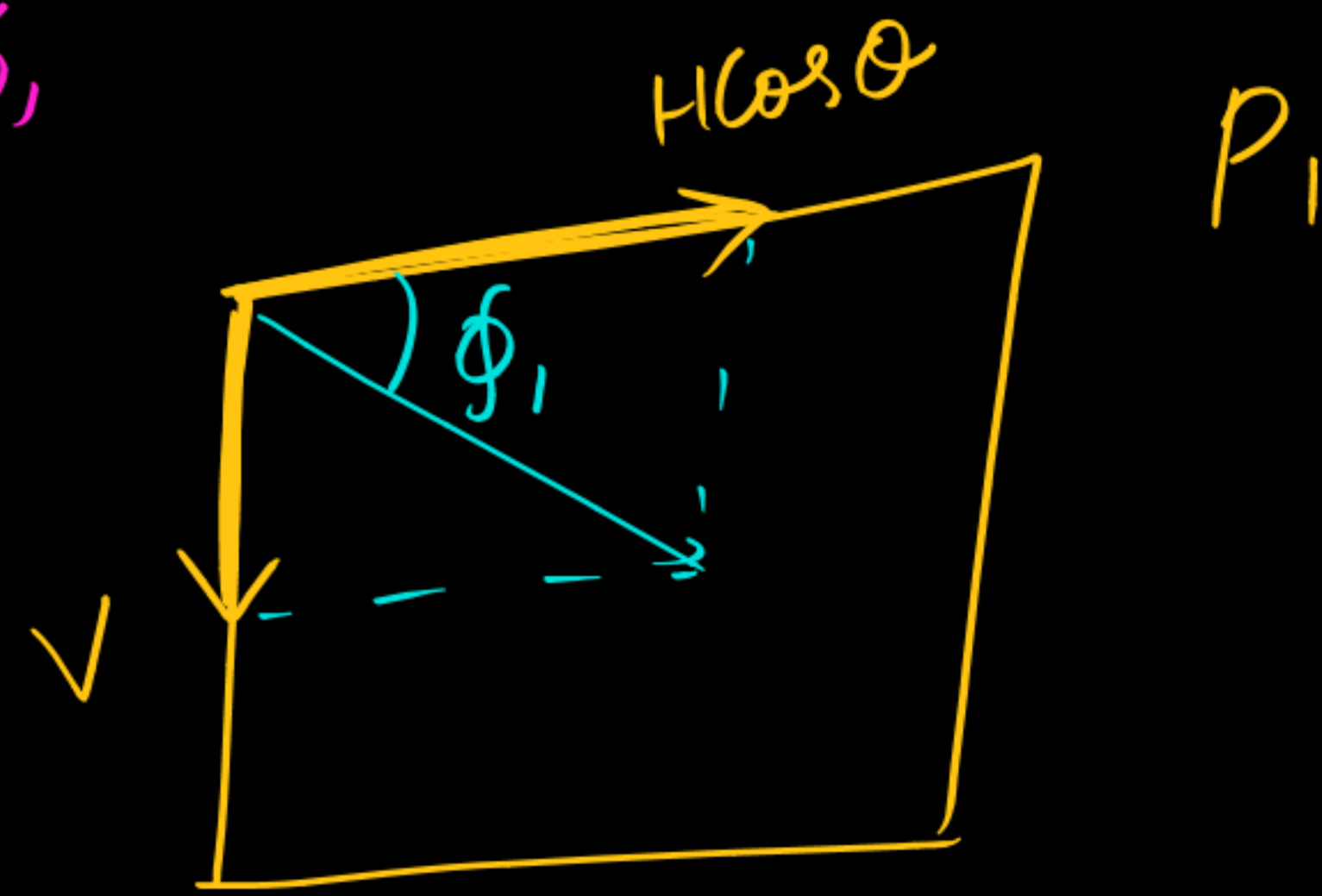
$\sin \theta = \frac{\tan \phi}{\tan \phi_2}$

$$1 = \frac{\tan^2 \phi}{\tan^2 \phi_1} + \frac{\tan^2 \phi}{\tan^2 \phi_2} \Rightarrow \frac{1}{\tan^2 \phi} = \frac{1}{\tan^2 \phi_1} + \frac{1}{\tan^2 \phi_2}$$





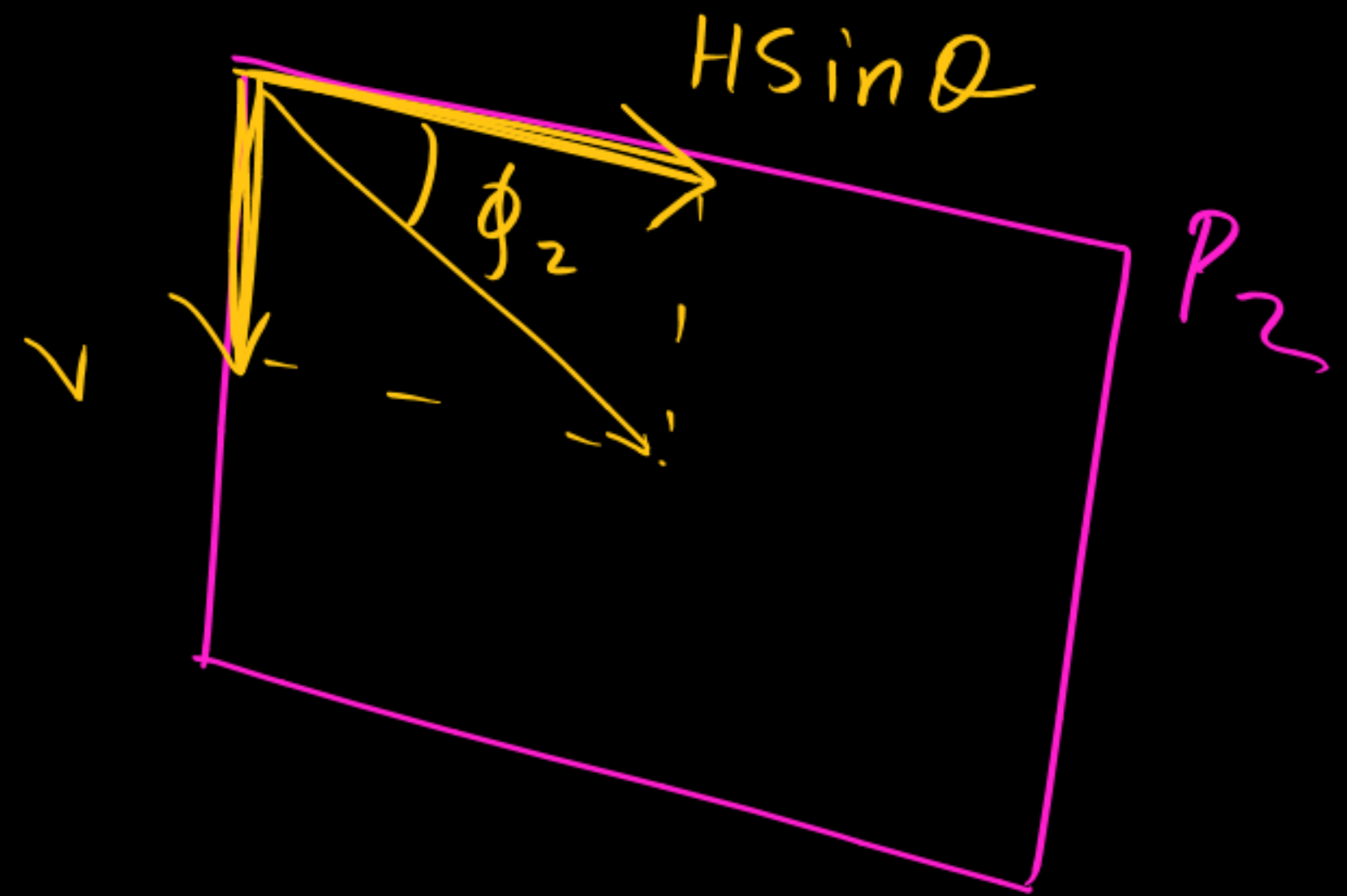
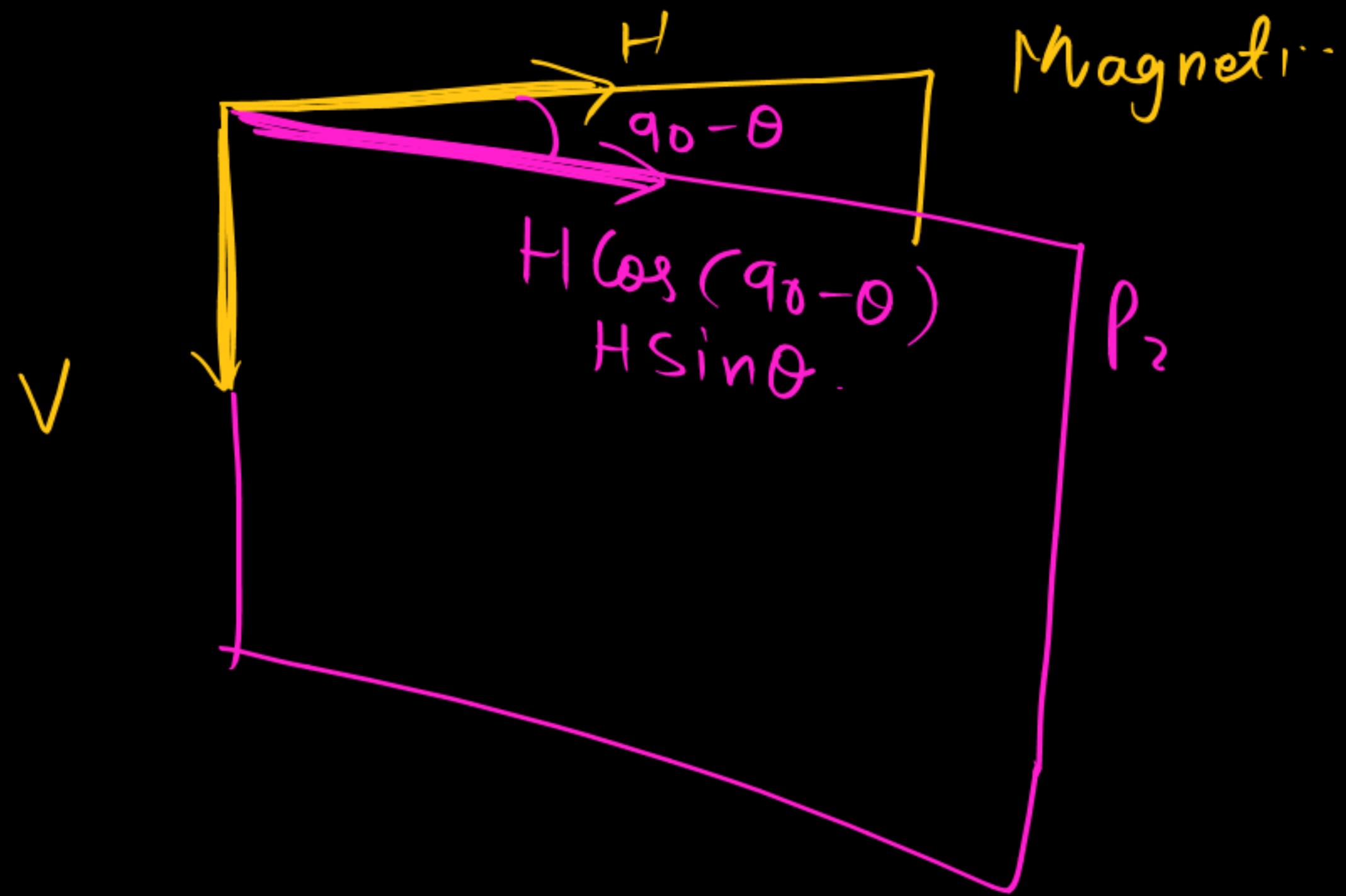
$$\tan \phi = \frac{V}{H}$$



$$\tan \phi_1 = \frac{V}{H \cos \theta}$$

$$\tan \phi_1 = \frac{\tan \phi}{\cos \theta}$$





$$\tan \phi_2 = \frac{V}{H \sin \theta}$$

$$\tan \phi_2 = \frac{\tan \phi}{\sin \theta}$$

*Thank You Lakshyians*