# MATHS JEE MAINS & ADVANCED **CLASS - XII** MODULE

Relations & Function | Inverse Trigonometric Functions Continuity & Differentiability, Methods of Differentiation **Application of Derivatives** Video solution will be

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# **EDITION : 2021**

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# JEE-MAIN PREVIOUS YEAR'S

RELATIONS

Q.1 If  $R = \{(x, y); x, y \in Z, x^2 + 3y^2 \le 8\}$  is a relation on the set of integers Z, then the domain of  $R^{-1}$  is : [JEE Main-2020 (September)] (1)  $\{0, 1\}$ (2)  $\{-2, -1, 1, 2\}$ 

$(1)$ {0, 1}	$(2)$ $\{-2, -1, 1, 2\}$
$(3) \{-1, 0, 1\}$	$(4) \{-2, -1, 0, 1, 2\}$

- **Q.2** Let  $R_1$  and  $R_2$  be two relation defined as follows :
  - [JEE Main-2020 (September)]
  - $R_1 = \{(a, b) \in \mathbb{R}^2 : a^2 + b^2 \in \mathbb{Q}\}$  and
  - $R_2 = \{(a,b) \in R^2 : a^2 + b^2 \in Q\}$ , where Q is the set of the rational numbers. Then :
  - (1) Neither  $R_1$  nor  $R_2$  is transitive.
  - (2)  $R_2$  is transitive but  $R_1$  is not transitive
  - (3)  $R_1^2$  and  $R_2$  are both transitive.
  - (4)  $R_1^1$  is transitive but  $R_2$  is not transitive.

## **FUNCTION**

**Q.3** If 
$$f(x) + 2f\left(\frac{1}{x}\right) = 3x, x \neq 0$$
 and

$$S = \{x \in R : f(x) = f(-x)\}$$
; then S:  
[JEE Main -2016]

(1) is an empty set.

- (2) contains exactly one element
- (3) contains exactly two elements
- (4) contains more than two elements

Q.4 The function 
$$f: \mathbb{R} \rightarrow \left[-\frac{1}{2}, \frac{1}{2}\right]$$
 defined as  $f(x) = \frac{x}{1+x^2}$ ,  
is: [JEE Main - 2017]  
(1) neither injective nor surjective.  
(2) invertible.  
(3) injective but not surjective.  
(4) surjective but not injective

 $\textbf{Q.5} \qquad \text{Let } S = \{x \in R : x \ge 0 \text{ and }$ 

$$2 |\sqrt{x} - 3| + \sqrt{x}(\sqrt{x} - 6) + 6 = 0$$
}. Then S:  
[JEE Main - 2018]

- (1) contains exactly one element.
- (2) contains exactly two elements.
- (3) contains exactly four elements.
- (4) is an empty set.

Q.6 For  $x \in R-[0, 1]$ , let  $f_1(x) = \frac{1}{x}, f_2(x) = 1-x$  and

 $f_3(x) = \frac{1}{1-x}$  be three given functions. If a function, J(x) satisfies  $(f_2 \circ J \circ f_1)(x) = f_3(x)$  then J(x) is equal to : [JEE Main - 2019 (January)]

(1) 
$$f_3(x)$$
 (2)  $\frac{1}{x} f_3(x)$  (3)  $f_2(x)$  (4)  $f_1(x)$ 

Let  $A = \{x \in R : x \text{ is not a positive integer}\}$  Define a

function 
$$f: A \to R$$
 as  $f(x) = \frac{2x}{x-1}$  then f is

- (1) injection but nor surjective
- (2) not injective

Q.7

0.9

- (3) surjective but not injective
- (4) neither injective nor surjective

**Q.8** Let N be the set of natural numbers and two functions f and g be defined as  $f, g: N \rightarrow N$  such that

$$f(n) = \begin{cases} \frac{n+1}{2} & \text{if } n \text{ is odd} \\ \frac{n}{2} & \text{if } n \text{ is even} \\ \text{and } g(n) = n - (-1)^n. \text{ Then fog is:} \\ \text{[JEE Main - 2019 (January)]} \end{cases}$$

- (1) onto but not one-one.
- (2) one-one but not onto.
- (3) both one-one and onto.
- (4) neither one-one nor onto.

Let a function 
$$f: (0, \infty) \rightarrow (0, \infty)$$
 be defined by  $f(x) =$ 

- $\left|1-\frac{1}{x}\right|$ . Then f is: [JEE Main 2019 (January)]
- (1) not injective but it is surjective
- (2) injective only
- (3) neither injective nor surjective
- (4) both injective as well as surjective
- Q.10 Let  $f_k(x) = \frac{1}{k} (\sin^k x + \cos^k x)$  for k = 1, 2, 3... Then for all  $x \in \mathbb{R}$ , the value of  $f_4(x) f_6(x)$  is equal to : [JEE Main - 2019 (January)] (1) 1/12 (2) 1/4 (3) -1/12 (4) 5/12 O.11 Let  $f(x) = a^x (a > 0)$  be written as  $f(x) = f_1(x) + f_2(x)$ , where

Let  $f(\mathbf{x}) = a^{\mathbf{x}} (a > 0)$  be written as  $f(\mathbf{x}) = f_1(\mathbf{x}) + f_2(\mathbf{x})$ , where  $f_1(\mathbf{x})$  is an even function of  $f_2(\mathbf{x})$  is an odd function. Then  $f_1(\mathbf{x} + \mathbf{y}) + f_1(\mathbf{x} - \mathbf{y})$  equals **[JEE Main - 2019(April)]** (1)  $2f_1(\mathbf{x})f_1(\mathbf{y})$  (2)  $2f_1(\mathbf{x})f_2(\mathbf{y})$ (3)  $2f_1(\mathbf{x} + \mathbf{y})f_2(\mathbf{x} - \mathbf{y})$  (4)  $2f_1(\mathbf{x} + \mathbf{y})f_1(\mathbf{x} - \mathbf{y})$ 

**Relations and Function** 



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Q.12 Let 
$$\sum_{k=1}^{10} f(a+k) = 16(2^{10}-1)$$
, where the function  $f$   
satisfies  $f(x+y) = f(x) f(y)$  for all natural numbers x, y  
and  $f(1) = 2$  then the natural number 'a' is  
[JEE Main - 2019(April)]  
(1)4 (2)3 (3) 16 (4)2  
Q.13 If the function  $f: \mathbb{R} - \{1, -1\} \rightarrow A$  defined by  
 $f(x) = \frac{x^2}{1-x^2}$ , is surjective, then A is equal to  
[JEE Main - 2019(April)]  
(1)  $\mathbb{R} - [-1, 0)$  (2)  $\mathbb{R} - (-1, 0)$  (3)  $\mathbb{R} - \{-1\}$  (4)  $[0, \infty)$ 

- Q.15 Let  $f(x) = \log_e(\sin x)$ ,  $(0 \le x \le \pi)$  and  $g(x) = \sin^{-1}(e^{-x})$ ,  $(x \ge 0)$ . If  $\alpha$  is a positive real number such that  $a = (fog)'(\alpha)$  and  $b = (fog)(\alpha)$ , then :

[JEE Main - 2019(April)](1)  $a\alpha^2 - b\alpha - a = 0$ (2)  $a\alpha^2 + b\alpha - a = -2\alpha^2$ (3)  $a\alpha^2 + b\alpha + a = 0$ (4)  $a\alpha^2 - b\alpha - a = 1$ 

Q.16 For 
$$x \in \left(0, \frac{3}{2}\right)$$
, let  $f(x) = \sqrt{x}$ ,  $g(x) = \tan x$  and  
 $h(x) = \frac{1 - x^2}{1 + x^2}$ . If  $\phi(x) = ((hof)og)(x)$ , then  $\phi = \left(\frac{\pi}{3}\right)$  is  
equal to : [JEE Main - 2019(April)]

(1) 
$$\tan \frac{\pi}{12}$$
 (2)  $\tan \frac{7\pi}{12}$  (3)  $\tan \frac{11\pi}{12}$  (4)  $\tan \frac{5\pi}{12}$   
17 If  $g(x) = x^2 + x - 1$  and  $(gof)(x) = 4x^2 - 10x + 5$  the

Q.17 If 
$$g(x) = x^2 + x - 1$$
 and (gof) (x) =  $4x^2 - 10x + 5$ , then  
 $f\left(\frac{5}{4}\right)$  is equal to [JEE Main-2020 (January)]  
(1)  $\frac{1}{2}$  (2)  $\frac{-3}{2}$  (3)  $\frac{-1}{2}$  (4)  $\frac{3}{2}$ 

Q.18 The inverse function of  $f(x) = \frac{8^{2x} - 8^{-2x}}{8^{2x} + 8^{-2x}}$ ,  $x \in (-1, 1)$  is [JEE Main-2020 (January)]

(1) 
$$\frac{1}{4}\log_{e}\left(\frac{1+x}{1-x}\right)$$
(2) 
$$\frac{1}{4}\log_{e}\left(\frac{1-x}{1+x}\right)$$
(3) 
$$\frac{\log_{8}e}{4}\log_{e}\left(\frac{1+x}{1-x}\right)$$
(4) 
$$\frac{\log_{8}e}{4}\log_{e}\left(\frac{1-x}{1+x}\right)$$

Q.19 Let 
$$f: R \to R$$
 be a function which satisfies  $f(x + y) = f(x)$   
+  $f(y) \forall x, y R$ . If  $f(1) = 2$  and  $g(n) = \sum_{k=1}^{(n-1)} f(k), n \in N$   
then t he value of n, for which  $g(n) = 20$ , is :

[JEE Main-2020 (September)]

Q.20 The domain of the function 
$$(|x|+5)$$

$$f(x) = \sin^{-1} \left( \frac{|x|+3}{x^2+1} \right)$$
is  
(-\infty, -a]  $\cup$  [a,\infty). Then a is equal to :  
[JEE Main-2020 (September)]

Q.21 Let  $A = \{a, b, c\}$  and  $B = \{1, 2, 3, 4\}$ . Then the number of elements in the set  $C = \{f: A \rightarrow B \mid 2 \in f(A) \text{ and } f \text{ is not one-one}\}$  is \_\_\_\_\_.

# [JEE Main-2020 (September)]

**Q.22** For a suitably chosen real constant a, let a function, f:

 $R - \{-a\} \rightarrow R$  be defined by  $f(x) = \frac{a-x}{a+x}$ . Further suppose that for any real number  $x \neq -a$  and  $f(x) \neq -a$ ,

$$(fof)(x) = x$$
. Then  $f\left(-\frac{1}{2}\right)$  is equal to :  
[JEE Main-2020 (September)]

(1)-3 (2) 
$$\frac{1}{3}$$
 (3)  $-\frac{1}{3}$  (4) 3

Q.23 If {p} denotes the fractional part of the number p, then 
$$\left\{\frac{3^{200}}{8}\right\}$$
, is equal to :

### [JEE Main-2020 (September)]

(1) 
$$\frac{5}{8}$$
 (2)  $\frac{1}{8}$  (3)  $\frac{7}{8}$  (4)  $\frac{3}{8}$ 

Q.24 If 
$$f(x+y) = f(x) f(y)$$
 and  $\sum_{x=1}^{\infty} f(x) = 2, x, y \in N$ ,

Where N is the set of all natural numbers, then the value of  $\frac{f(4)}{f(2)}$  is :

ue of 
$$\frac{1}{f(2)}$$
 is :

#### [JEE Main-2020 (September)]

(1) 
$$\frac{1}{9}$$
 (2)  $\frac{4}{9}$  (3)  $\frac{1}{3}$  (4)  $\frac{2}{3}$ 

#### JEE-ADVANCED PREVIOUS YEAR'S

Q.1 Let  $f(x) = x^2$  and  $g(x) = \sin x$  for all  $x \in \mathbb{R}$ . Then the set of all x satisfying (f o g o g o f) (x) = (g o g o f) (x), where (f o g) (x) = f(g(x)), is [IIT JEE - 2011] (A)  $\pm \sqrt{n\pi}$ ,  $n \in \{0, 1, 2, ....\}$ (B)  $\pm \sqrt{n\pi}$ ,  $n \in \{1, 2, ....\}$ (C)  $\frac{\pi}{2} + 2n\pi$ ,  $n \in \{...., -2, -1, 0, 1, 2, ....\}$ (D)  $2n\pi$ ,  $n \in \{...., -2, -1, 0, 1, 2, ....\}$ 

Q.2 The function  $f: [0, 3] \rightarrow [1, 29]$ , defined by  $f(x)=2x^3-15x^2+36x+1$ , is [IIT JEE-2012] (A) one-one and onto (B) onto but not one-one (C) one-one but not onto (D) neither one-one nor onto

**Relations and Function** 

Q.3 Let  $f: (-1, 1) \to IR$  be such that  $f(\cos 4\theta) = \frac{2}{2 - \sec^2 \theta}$  Q.5 for  $\theta \in \left(0, \frac{\pi}{4}\right) \cup \left(\frac{\pi}{4}, \frac{\pi}{2}\right)$ . Then the value(s) of  $f\left(\frac{1}{3}\right)$ is (are) [IIT JEE-2012]

(A) 
$$1 - \sqrt{\frac{3}{2}}$$
 (B)  $1 + \sqrt{\frac{3}{2}}$  (C)  $1 - \sqrt{\frac{2}{3}}$  (D)  $1 + \sqrt{\frac{2}{3}}$ 

**Q.4** Let f:  $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right) \rightarrow R$  be given by

 $f(x) = (\log(\sec x + \tan x))^3$ . Then **[JEEAdvanced-2014]** (A) f(x) is an odd function (B) f(x) is a one-one function

(C) f(x) is an onto function

(D) 
$$f(x)$$
 is an even function

If  $\alpha = 3\sin^{-1}\left(\frac{6}{11}\right)$  and  $\beta = 3\cos^{-1}\left(\frac{4}{9}\right)$ , where the

inverse trigonometric functions take only the principal values, then the correct option(s) is(are) [JEE Advanced-2015]

(A) 
$$\cos \beta > 0$$
 (B)  $\sin \beta < 0$   
(C)  $\cos(\alpha + \beta) > 0$  (D)  $\cos \alpha < 0$ 

Q.6

Let the function  $f : [0,1] \rightarrow \mathbb{R}$  be defined by

$$f(x) = \frac{4^{x}}{4^{x} + 2}$$
  
Then the value of  
$$f\left(\frac{1}{40}\right) + f\left(\frac{2}{40}\right) + f\left(\frac{3}{40}\right) + \dots + f\left(\frac{39}{40}\right) - f\left(\frac{1}{2}\right)$$
 is ....  
[JEE(Advanced) - 2020]

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# **ABOUT PHYSICS WALLAH**

Alakh Pandey is one of the most renowned faculty in NEET & JEE domain's Physics. On his YouTube channel, Physics Wallah, he teaches the Science courses of 11th and 12th standard to the students aiming to appear for the engineering and medical entrance exams.

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