

Name _____

Quiz Section _____

In this work sheet we'll study the technique of integration by parts. Recall that the basic formula looks like this:

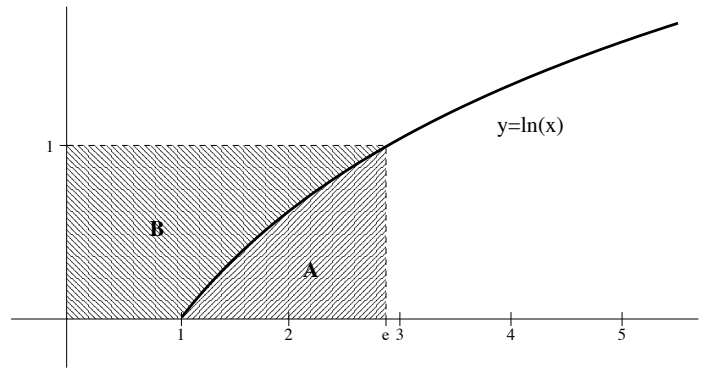
$$\int u dv = u \cdot v - \int v du$$

1 First a warm-up problem. Consider the integral $\int x \sin(3x) dx$. Let $u = x$ and let $dv = \sin(3x) dx$. Compute du by differentiating and v by integrating, and use the basic formula to compute the original integral. Don't forget the arbitrary constant!

2 Compute $\int \ln x dx$. (The proper technique is, indeed, integration by parts. What should you take to be u and dv ? The choices are pretty limited. Try one and see what happens.)

3 The regions A and B in the figure are revolved around the x -axis to form two solids of revolution.

(a) Before computing the integrals, which solid do you think has a larger volume? Why?



(b) Use the disk method to find the volume of the solid swept out by region A .

(c) Use the shell method to find the volume of the solid swept out by region B .

4 Suppose we try to integrate $1/x$ by parts, taking $u = 1/x$ and $dv = dx$. We have $du = (-1/x^2) dx$ and $v = x$, so

$$\begin{aligned}\int \frac{1}{x} dx &= \frac{1}{x} \cdot x - \int x \cdot \frac{-1}{x^2} dx \\ &= 1 + \int \frac{1}{x} dx.\end{aligned}$$

Canceling the integral from both sides, we get the disconcerting result that $0 = 1$. *What went wrong?* What happens if we replace the indefinite integrals by definite integrals, that is, if we try to calculate $\int_a^b \frac{1}{x} dx$ by this method?