

1. (a)  $\frac{d}{dx} \left[ e^{\sin(\sqrt{e^x})} \right]$

(b)  $\frac{d}{dx} \left[ \sin(\cos(\tan(x^{3/2} + x))) \right]$

(c)  $\frac{d}{dx} \left[ x e^{(x e^x)} \right]$

2.  $x(t) = \cos(2t)$  and  $y(t) = \sin(3t)$ . Find the equations of the tangent lines at the  $y$  intercepts.

3. Let  $f$  and  $g$  be positive differentiable functions and  $a$  and  $b$  positive real numbers.

(a) Write a formula in terms of  $f$  and  $g$  for  $\frac{d}{dx} \sqrt{f(g(x))}$ .

(b) Suppose that  $f(a) = b$  and  $\frac{d}{dx} \sqrt{f(ax)} = \sqrt{b}$ . Write a formula for  $f'(a)$ .  
*Hint: Use part (a) and let  $x = 1$ .*

(c) When  $x = a$  write the equation (involving  $a$  and  $b$ ) for the tangent line to  $f$ .

(d) Write  $f(x)$  as a formula involving  $a$  and  $b$ . (*Difficult.*)

4. A curve  $\Gamma$  is defined by  $x^2y + y^2x + 2x + y = \pi$ . Find  $\frac{dy}{dx}$ .

5. Let  $C$  be the curve defined by the relation

$$\sin(x^2 + y^2) = e^{2y}$$

(a) Find  $\frac{dy}{dx}$  for  $C$ .

(b) Find the equation of the tangent line to  $C$  at the point  $(x, y) = (\sqrt{\pi}, 0)$ .

(c) Use the tangent line at  $(\sqrt{\pi}, 0)$  to estimate the number  $a$  so that  $(a, \frac{\pi}{10})$  lies on  $C$ .

6. A marble rolls on a flat table along the curve

$$y \ln(xy) = e^{2x-1}$$

At the point  $(1, e)$  the  $y$ -coordinate of the marble is changing at  $\pi$  cm/sec. At what rate is the  $x$ -coordinate changing? *Hint: differentiate with respect to  $t$ .*