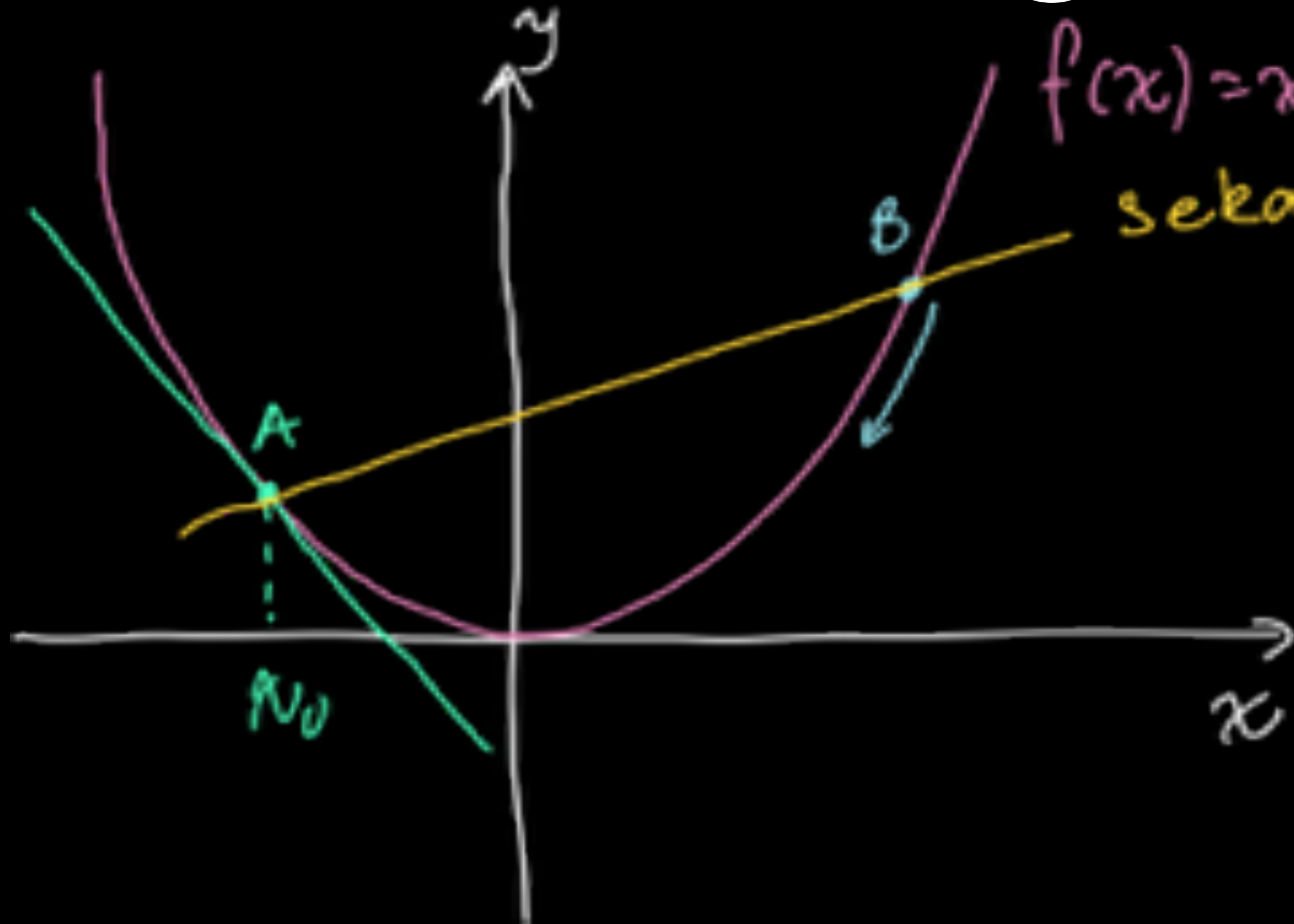


SEKANTER

TANGENTER

OG TRETRINSREGLEN

Sekanter og tangenter



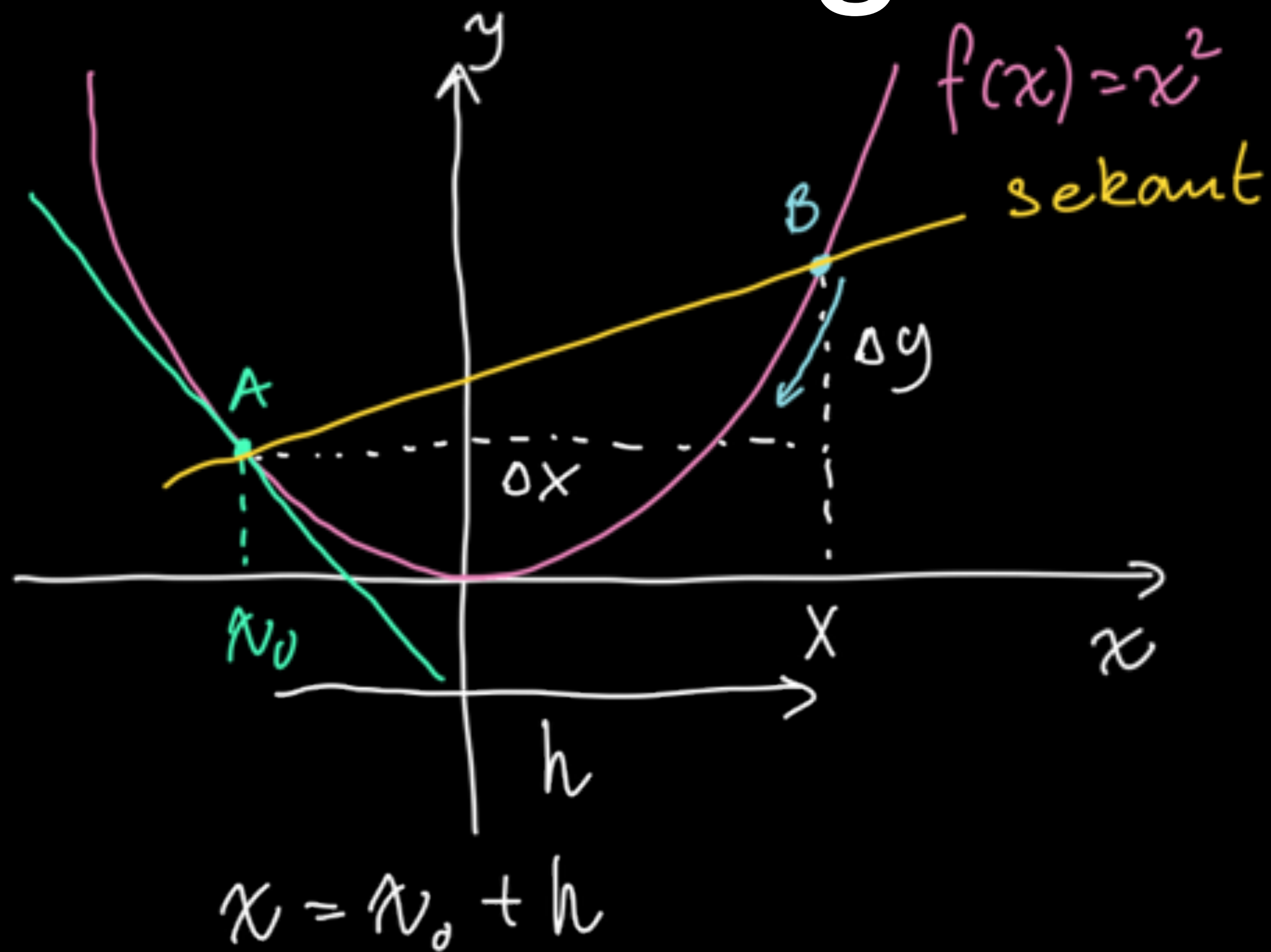
$$f(x) = x^2$$

sekant

$$a = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$



Tretrinsregeln



$$\textcircled{1} \Delta y = f(x_0 + h) - f(x_0)$$

$$\textcircled{2} \frac{\Delta y}{\Delta x} = \frac{f(x_0 + h) - f(x_0)}{h}$$

differenzquotient

$$\textcircled{3} \lim_{h \rightarrow 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

Eksempel

$$f(x) = x^2$$

$$\textcircled{1} \Delta y = f(x_0 + h) - f(x_0)$$

$$\textcircled{2} \frac{\Delta y}{\Delta x} = \frac{f(x_0 + h) - f(x_0)}{h}$$

$$\textcircled{3} \lim_{h \rightarrow 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

$$\textcircled{1} \Delta y = (x_0 + h)^2 - x_0^2 \quad (a+b)^2 = a^2 + b^2 + 2ab$$
$$= \cancel{x_0^2} + h^2 + 2x_0h - \cancel{x_0^2}$$
$$= h^2 + 2x_0h$$

$$\textcircled{2} \frac{\Delta y}{\Delta x} = \frac{h^2 + 2x_0h}{h} = h + 2x_0$$

$$\textcircled{3} \lim_{h \rightarrow 0} h + 2x_0 = 2x_0 + "0" = 2x_0$$

$$f'(x) = 2x$$

$f'(x)$

f merke af x
afledte funktion
differenskvotient