

# Slicing the Pie: Quantifying the Aggregate and Distributional Effects of Trade

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# Motivation

- Gravity models → quantify *aggregate* welfare effects of trade
- Empirical research → large *distributional* effects of trade
- How large are the aggregate gains from trade and how are they distributed?
- This paper:
  - ▶ Theoretical framework for the gains from trade and their distribution
  - ▶ GE structure for the literature on the distributional effects of trade

## Overview: theory

- Framework to jointly understand and quantify the aggregate and distributional effects of trade
- Building blocks:
  - ▶ Multi-sector gravity model of trade (EK, CDK, ACR)
  - ▶ Roy-Fréchet model of labor allocation across sectors (LW)
  - ▶ Various groups of ex-ante identical workers (HHJK, BMV)
- Analytical expressions for aggregate and group-level welfare effects
- Mechanisms:
  - ▶ Aggregate effects arise from inter- and intra-sectoral trade
  - ▶ Between-group distributional impact has specific-factors intuition

## Application to local labor markets

- Methodology applicable to groups by age, gender, location, etc.
  - ▶ Focus on application to groups by education and, in particular, location
- GE structure for empirical literature on trade and local labor markets
  - ▶ Exercise based on data for commuting zones x skill groups in the US
  - ▶ Link to Autor, Dorn and Hanson (2013 - ADH)
- Focus on baseline version of the model
  - ▶ Model with all goods tradable across groups
  - ▶ Most parsimonious version of the model
  - ▶ Extensions do not change essential features of baseline model

## Limitations of baseline model

1. No movement of labor out of tradable sectors – extension
2. No intermediate goods - extension
3. No mobility across groups - extension
4. No costs of trade across groups - can relax
5. Strong parametric assumptions - can relax
6. No implications for within-group inequality
7. No dynamics

# Model

# Model

- $N$  countries, index  $i, j$
- $S$  sectors, index  $s, k$
- $G$  groups, index  $g$

## Model: Trade Side

- Each sector is modeled as in EK:
  - ▶ Continuum of goods in  $[0, 1]$ , CES preferences with EoS  $\sigma_s$
  - ▶ National CRS technologies drawn iid-Fréchet with  $T_{is}$  and  $\theta_s > \sigma_s - 1$
  - ▶ Iceberg trade costs  $\tau_{ijs} \geq 1$
- Preferences across sectors are Cobb-Douglas with shares  $\beta_{is}$
- Expenditure shares:

$$\lambda_{ijs} = \frac{T_{is} (\tau_{ijs} w_{is})^{-\theta_s}}{\gamma^{-\theta_s} P_{js}^{-\theta_s}}$$

where  $\gamma^{-\theta_s} P_{js}^{-\theta_s} = \sum_l T_{ls} (\tau_{ljs} w_{ls})^{-\theta_s}$



## Model: Labor Side

- Exogeneous mass  $L_{ig}$  of workers of type  $g$  in country  $i$
- A worker from  $g$  has efficiency units  $z$  in  $s$  drawn iid from a Fréchet dist. with  $\kappa > 1$  and  $A_{igs}$
- $w_{is}$  is the wage per efficiency unit in sector  $s$  of country  $i$ 
  - ▶  $w_{is}$  same across  $g$ : national  $p_{iis}$ ,  $T_{is}$
  - ▶  $w_{is}$  can differ across  $s$ : upward sloping labor supply to each  $s$
- Results: share of workers in group  $g$  who choose to work in sector  $s$  is

$$\pi_{igs} = \frac{A_{igs} w_{is}^\kappa}{\Phi_{ig}^\kappa} \text{ with } \Phi_{ig} \equiv \left( \sum_k A_{igk} w_{ik}^\kappa \right)^{1/\kappa}$$

## Labor Market Equilibrium

- Demand for efficiency units in sector  $s$  in country  $i$  is (cfr. EK)

$$\frac{1}{w_{is}} \sum_j \lambda_{ijs} \beta_{js} Y_j,$$

- Share of workers in group  $g$  that choose to work in sector  $s$  is (cfr. LW)

$$\pi_{igs} = \frac{A_{igs} w_{is}^\kappa}{\Phi_{ig}^\kappa} \text{ with } \Phi_{ig} \equiv \left( \sum_k A_{igk} w_{ik}^\kappa \right)^{1/\kappa}$$

- Equilibrium: find  $w_{is}$  that equalize demand and supply of efficiency units.
  - ▶ Equations
  - ▶ Graphically
- Comparative statics: “exact hat algebra” (DEK) to compute counterfactual  $\hat{\lambda}_{ijs}$  and  $\hat{\pi}_{igs}$

## Comparative Statics: Welfare

- Define  $y_{ig} = \frac{Y_{ig}}{L_{ig}}$ . Given all  $\widehat{w}_{is}$  we can get  $\widehat{\lambda}_{iis}$  and  $\widehat{\pi}_{igs}$  and then

$$\begin{aligned}
 \widehat{y}_{ig} / \widehat{P}_i &= \widehat{\Phi}_{ig} / \widehat{P}_i \text{ (from } y_{ig} = \eta \Phi_{ig} \text{ )} \\
 &= \widehat{\Phi}_{ig} / \prod_s \widehat{P}_{is}^{\beta_{is}} \text{ (Cobb-Douglas preferences)} \\
 &\text{from } \lambda_{iis} = \frac{T_{is} W_{is}^{-\theta_s}}{\eta^{\theta_s} P_{is}^{-\theta_s}} \text{ and } \pi_{igs} = \frac{A_{igs} W_{is}^{\kappa}}{\Phi_{ig}^{\kappa}} : \\
 &= \underbrace{\prod_s \widehat{\lambda}_{iis}^{-\beta_{is}/\theta_s}}_{\text{Multi-sector ACR}} \cdot \underbrace{\prod_s \widehat{\pi}_{igs}^{-\beta_{is}/\kappa}}_{\text{Group-level "Roy" term}}
 \end{aligned}$$

## Empirical Analysis and Estimation of $\kappa$

# Data

- For  $i = \text{US}$ , sector  $s$
- US Labor Market:
  - ▶ Census and ACS data
  - ▶ Group employment shares at the Commuting Zone (CZ)-Skill level
  - ▶  $G = 1,444$  (722 CZs  $\times$  2 skill groups)
  - ▶  $S = 14$ , with 13 manufacturing sectors and 1 non-manufacturing sector
  - ▶ Time period: 2000 - 2011
- Trade data from WIOD

## The rise of China as a trade shock

- Identification as in ADH:
  - ▶ The “rise of China” is an exogenous supply shock that affects all developed economies in similar fashion.
- Import-penetration variable in the style of ADH for each  $s \in M$ :

$$\Delta IP_s^{China \rightarrow Other} \equiv \frac{\Delta M_s^{China \rightarrow Other}}{L_{US,s}}$$

- ▶  $\Delta M_s^{China \rightarrow Other}$  : change in imports of “Other” from “China”
  - ▶ “Other” is set of developed countries similar to US (as in ADH).
  - ▶  $L_{US,s}$  is the level of employment in the US in sector  $s$ , in 2000
- Our instrument is a Bartik (1991)-type variable:

$$\sum_{s \in M} \pi_{gs}^M \Delta IP_s^{China \rightarrow Other}$$

## Structural estimation of $\kappa$

- From  $\hat{\pi}_{igs} = \frac{\hat{A}_{igs} \hat{w}_{is}^\kappa}{\hat{\Phi}_{ig}^\kappa}$ , for all sectors  $s$ :

$$\hat{y}_g = \hat{w}_s \hat{\pi}_{gs}^{-1/\kappa} \hat{A}_{gs}^{1/\kappa}$$

- Focusing on the non-manufacturing (NM) sector and taking logs:

$$\ln \hat{y}_g = \alpha - \frac{1}{\kappa} \ln \hat{\pi}_{gNM} + \varepsilon_g$$

- ▶ Where  $\alpha \equiv \ln \hat{w}_{NM}$ ,  $\varepsilon_g \equiv \ln \hat{A}_{gNM}^{1/\kappa}$
- ▶ Use the Bartik China-shock as an instrument for  $\ln \hat{\pi}_{gNM}$

Table: Estimation of  $\kappa$ 

	Dependent variable: $\ln \hat{y}_g$		
	(1)	(2)	(3)
	Workers	Hours	Earnings
$\ln \hat{\pi}_{gNM}$	-0.466 (0.161)	-0.494 (0.166)	-0.512 (0.181)
Implied $\kappa$	2.147 (0.743)	2.024 (0.682)	1.952 (0.689)
First-stage F-Statistic	23.19	20.43	9.902
Observations	1444	1444	1444

IV-estimation results where  $y_g$  is measured as average earnings per worker, and  $\pi_{gNM}$  is the labor share employed in non-manufacturing. Labor shares  $\pi_{gs}$  are measured as the share of workers, share of labor hours and share of earnings for columns 1, 2 and 3 respectively. Conley standard errors (in parentheses), with a cutoff for the spatial correlation at approximately 400km.



## Model-based Bartik measure of import competition

- For  $\kappa \rightarrow 1$ , the data provides sufficient statistics for group-level gains from trade
- In this case,

$$\frac{\widehat{Y}_{ig}^A}{\widehat{Y}_i^A} = l_{ig} \equiv \sum_s \pi_{igs} \frac{\beta_{is}}{r_{is}}$$

with  $r_{is} \equiv \sum_g \pi_{igs} Y_{ig} / Y_i$

- For any foreign shock, if  $\kappa \rightarrow 1$

$$\ln \widehat{Y}_{ig} / \widehat{Y}_i = \ln \sum_s \pi_{igs} \widehat{r}_{is} = \ln \widehat{l}_{ig}$$

## Taking the Bartik measure to the data

- Bartik measure of import competition:

$$\ln \hat{Y}_{ig} / \hat{Y}_i \approx \ln \sum_s \pi_{igs} \hat{r}_{is}$$

- ▶ This relationship is exact for  $\kappa \rightarrow 1$ , and almost exact for  $\kappa > 1$

Simulation results

- Test empirical relationship for the China shock:

$$\ln \hat{y}_g = \alpha + \beta \ln \sum_s \pi_{gs} \hat{r}_s + \varepsilon_g$$

- ▶ Use the Bartik China-shock as an instrument for  $\ln \sum_s \pi_{gs} \hat{r}_s$
- Using counterfactual simulations, we can examine the relationship between  $\kappa$  and  $\beta$ : Simulation results
- We find  $\beta \approx 1/\kappa$ , so our estimates imply a value of  $\kappa$  around 1.5

(a) First Stage:  $\ln \sum_s \pi_{gs} \hat{r}_s = \alpha + \beta \sum_{s \in M} \pi_{gs}^M \Delta IP_{st}^{China \rightarrow Other} + \varepsilon_g$

	(1)	(2)	(3)
	Workers	Hours	Earnings
$\sum_{s \in M} \pi_{gs}^M \Delta IP_{st}^{China \rightarrow Other}$	-0.00348 (0.000982)	-0.00779 (0.00218)	-0.00151 (0.000505)
F Statistic	12.52	12.71	8.924

(b) Second Stage:  $\ln \hat{y}_g = \alpha + \beta \ln \sum_s \pi_{gs} \hat{r}_s + \varepsilon_g$

	(1)	(2)	(3)
$\ln \sum_s \pi_{gs} \hat{r}_s$	0.712 (0.228)	0.703 (0.221)	0.648 (0.212)
Observations	1444	1444	1444

$y_g$  is measured as average earnings per worker and the  $\pi_{gs}$  are measured as the share of workers, share of labor hours and share of earnings for columns 1, 2 and 3 respectively. Conley SEs (in parentheses) have a cutoff for the spatial correlation at ca. 400km.

# Counterfactual Analysis

# Overview of counterfactuals

- Throughout,  $\theta_s = 5$ , as in Head & Mayer (2014)
- Return to autarky for the United States: Autarky Results
  - ▶ Gains from trade are 1.52%, with coefficient of variation of 33%.
  - ▶ Some groups lose substantially from free trade, and trade increases inequality.
- Next: the “rise of China”

## China-shock calibration

- Calibration of  $\widehat{T}_{China,s}$ 
  - ▶ Inspired by Caliendo, Dvorkin & Parro (2016)
- Run a variation on ADH's first-stage regression for our data

$$\widehat{\lambda}_{China,US,s} = \alpha + \beta \widehat{\lambda}_{China,Other,s} + \varepsilon_s$$

- ▶ Obtain  $\widehat{\lambda}_{China,US,s} \equiv \widehat{\beta} \widehat{\lambda}_{China,Other,s}$
- ▶ Calibrate  $\widehat{T}_{China,s}$  to fit the simulated  $\widehat{\lambda}_{China,US,s}$  to  $\widehat{\lambda}_{China,US,s}$

## Simulated China shock and groups' income changes

$\kappa$	$\widehat{W}_{US}$	Mean	CV	Min.	Max.	$\prod_s \widehat{\lambda}_s^{-\beta_s/\theta_s}$
→ 1	0.29	0.38	0.87	-2.24	2.56	0.20
2	0.25	0.32	0.56	-1.64	1.34	0.20
4	0.23	0.28	0.36	-1.01	0.76	0.21
→ ∞	0.24	0.24	0.00	0.24	0.24	0.24

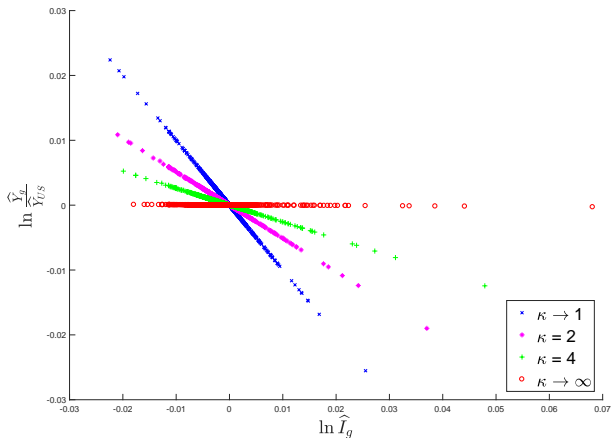
The first column displays the aggregate welfare effect of the China shock for the US, in percentage terms ( $100(\widehat{W}_{US} - 1)$ ), and the second column shows the mean welfare effect:

$100(\frac{1}{G} \sum_g \widehat{W}_{US,g} - 1)$ . The third column shows the coefficient of variation (CV), and for the fourth and fifth column we have  $\text{Min.} \equiv \min_g 100(\widehat{W}_{US,g} - 1)$  and  $\text{Max.} \equiv \max_g 100(\widehat{W}_{US,g} - 1)$ , respectively. The final column displays  $100 \left( \prod_s \widehat{\lambda}_{US,US,s}^{-\beta_{US,s}/\theta_s} - 1 \right)$ . The values for  $\hat{T}_{China,s}$  are

calibrated for  $\kappa = 2$ .

[Back](#)

# China simulations: Bartik measure of import competition



- For  $\kappa \rightarrow 1$ ,  $\widehat{Y}_{ig} / \widehat{Y}_i = \sum_s \pi_{igs} \widehat{r}_{is}$ . Linear relation persists for  $\kappa > 1$ .

[Back](#)



## Theory: Inequality-Adjusted Welfare Effects

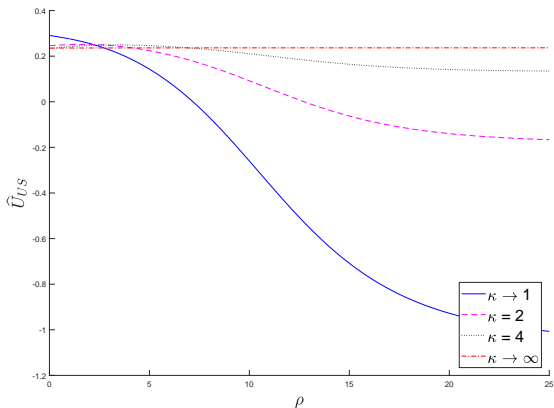
- Let  $W_{ig} \equiv Y_{ig}/P_i$ . Utility for agent behind the veil of ignorance

$$U_i \equiv \left( \sum_g \frac{L_{ig}}{L_i} W_{ig}^{1-\rho} \right)^{1/(1-\rho)}$$

- The higher  $\rho$ , the more risk (or inequality) averse
  - ▶ For  $\rho = 0$ ,  $U_i = W_i$ , with  $W_i \equiv \sum_g \frac{L_{ig}}{L_i} W_{ig}$
- Inequality-adjusted welfare effects:

$$\hat{U}_i$$

# Inequality-adjusted welfare effects



The figure plots the relationship between  $\hat{U}_i$ , the inequality-adjusted welfare effects of the rise of China, with  $U_i \equiv \left( \sum_g l_{ig} W_{ig}^{1-\rho} \right)^{1/(1-\rho)}$ , and  $\rho$  which is the coefficient of relative risk aversion for the agent behind the veil of ignorance.

## Conclusion

- Framework to jointly examine aggregate and distributional effects of trade
- The welfare effects are summarized in a parsimonious equation that nests the multi-sector ACR result
- In the data, we find:
  - ▶ An estimate of  $\kappa$  around 2
  - ▶ Which we validate with an indirect estimation of  $\kappa$  using our Bartik measure of import competition
- In the simulated model, we find:
  - ▶ that the China shock increases average welfare, but some groups experience losses as high as five times the average gain
  - ▶ Adjusted for plausible measures of inequality aversion, gains in social welfare are positive, and only slightly lower than with the standard aggregation.

# Equilibrium

- Excess demand for efficiency units in sector  $s$  of country  $i$  is

$$ELD_{is} \equiv \frac{1}{w_{is}} \sum_j \lambda_{ijs} \beta_{js} Y_j - \sum_g E_{igs}$$

- $\lambda_{ijs}$ ,  $Y_j$  and  $E_{igs}$  are functions of the whole matrix of wages  $\mathbf{w} \equiv \{w_{is}\}$ , so system  $ELD_{is} = 0$  for all  $i, s$  determines all wages  $\mathbf{w}$

## Comparative Statics: Wages

- Foreign shock:  $\hat{T}_{is}, \hat{\tau}_{ijs} \neq 1$  for  $i \neq j$  ( $\hat{x} \equiv x'/x$ )
- Using  $ELD_{is} = 0$ , we can write  $ELD'_{is} = 0$  as

$$\sum_g \hat{\pi}_{igs} \hat{\Phi}_{ig} \pi_{igs} Y_{ig} = \sum_j \hat{\lambda}_{ijs} \lambda_{ijs} \beta_{js} \sum_g \hat{\Phi}_{jg} Y_{jg}$$

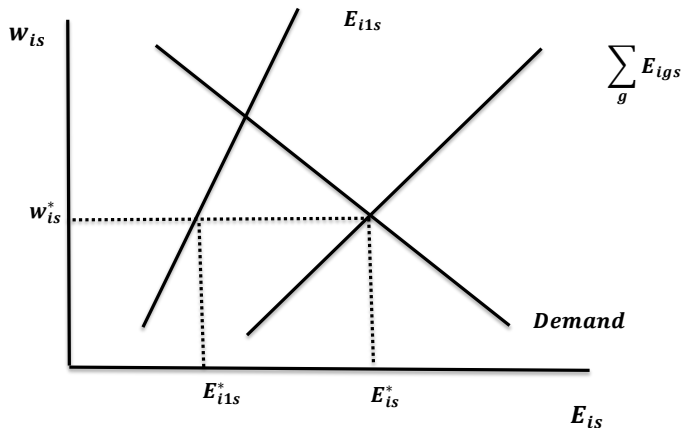
with

$$\hat{\Phi}_{ig} = \left( \sum_k \pi_{igk} \hat{w}_{ik}^\kappa \right)^{1/\kappa},$$

$$\hat{\lambda}_{ijs} = \frac{\hat{T}_{is} (\hat{\tau}_{ijs} \hat{w}_{is})^{-\theta_s}}{\sum_k \lambda_{kjs} \hat{T}_{ks} (\hat{\tau}_{kjs} \hat{w}_{ks})^{-\theta_s}},$$

$$\hat{\pi}_{igs} = \frac{\hat{w}_{is}^\kappa}{\sum_k \pi_{igk} \hat{w}_{ik}^\kappa}$$

## Supply and Demand of $E_{is}$



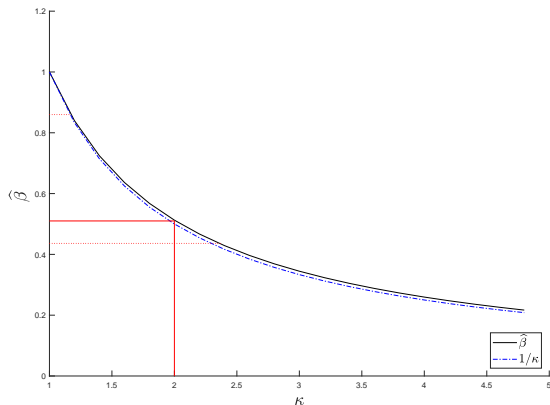
## First-stage estimation results

Table: Dependent variable:  $\ln \hat{\pi}_{gNM}$

	(1) Workers	(2) Hours	(3) Earnings
$\ln \sum_{s \in M} \pi_{gs}^M \Delta IP_{st}^{China \rightarrow Other}$	0.000330 (0.0000358)	0.000323 (0.0000366)	0.000296 (0.0000485)
P-value	2.76e-20	1.01e-18	1.05e-09
Observations	1444	1444	1444

$\pi_{gNM}$  is the labor share employed in non-manufacturing. Labor shares  $\pi_{gs}$  are measured as the share of workers, share of labor hours and share of earnings for columns 1, 2 and 3 respectively. Conley standard errors (in parentheses), with a cutoff for the spatial correlation at 500km.

## Bartik measure: regressions on simulated data



We regress  $\ln \hat{y}_g = \alpha + \beta \ln \sum_s \pi_{gs} \hat{r}_s + \varepsilon_g$  on simulated data and display the obtained  $\hat{\beta}$  for data generated for a given  $\kappa$ . [Back](#)



## The United States move to autarky

$\kappa$	$\widehat{W}_{US}$	Mean	CV	Min.	Max.	$\prod_s \widehat{\lambda}_s^{-\beta_s/\theta_s}$
→ 1	1.60	1.80	0.59	-7.86	3.36	1.45
2	1.52	1.63	0.33	-3.19	2.41	1.45
4	1.48	1.54	0.18	-0.87	1.93	1.45
→ $\infty$	1.45	1.45	0.00	1.45	1.45	1.45

The first column displays the aggregate gains from trade for the US, in percentage terms ( $100(1 - \widehat{W}_{US})$ ) and the second column shows the mean welfare effect:  $100(\frac{1}{G} \sum_g 1 - \widehat{W}_{US,g})$ . Here,  $\widehat{W}_{US}$  and  $\widehat{W}_{US,g}$  are the aggregate and group-level welfare change from a return to autarky for the US. The third column shows the coefficient of variation (CV), and for the fourth and fifth column we have  $\text{Min.} = \min_g 100(1 - \widehat{W}_{US,g})$  and  $\text{Max.} = \max_g 100(1 - \widehat{W}_{US,g})$ , respectively. The final column displays  $100 \left( 1 - \prod_s \widehat{\lambda}_{US,US,s}^{-\beta_{US,s}/\theta_s} \right)$ .

[Back to Overview](#)