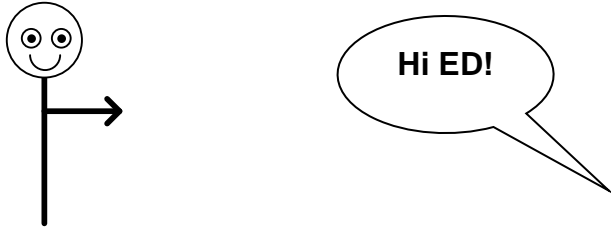


# Physics NYB problem set 5 solution

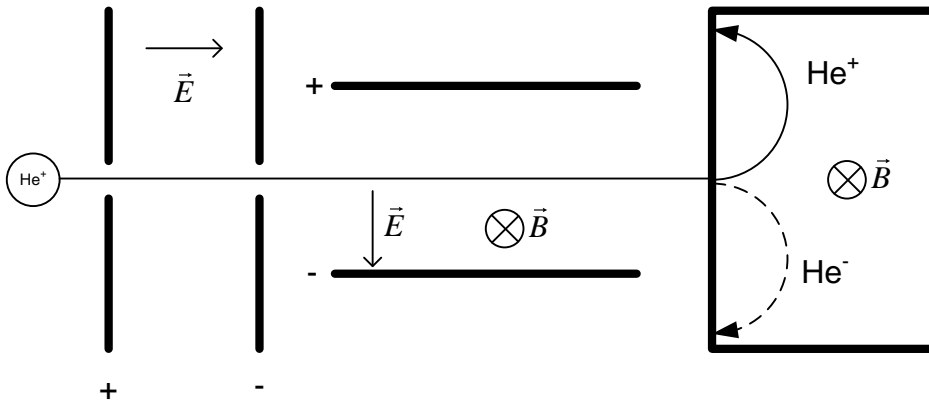
Hello everybody, this is ED☉.



ED is useful for drawing the right hand rule when you don't know how to draw. When you have a cross product such as  $\vec{C} = \vec{A} \times \vec{B}$ , ED lies along  $\vec{A}$ , looks along vector  $\vec{B}$  (note how his eyes ☉ are the symbol for a vector coming out of the page) and his left arm  $\longrightarrow$  points along vector  $\vec{C}$ .

## Part A

### Question A



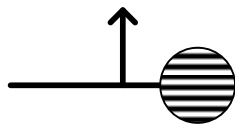
For part B, the electric force points down



Which means that the magnetic force points up



And by the right hand rule, (shown below) the magnetic field is in the page.



### Question B

A magnetic field can only exert a force on a moving particle, as we can see in the formula  $\vec{F} = q\vec{v} \times \vec{B}$ . So if a particle is initially at rest (i.e. not moving) the magnetic field cannot

exert a force, which means it cannot accelerate the particle, which means it cannot set the particle in motion.

Now I ask you: can a magnetic field stop a particle? (That would be a good one for a test, don't you think?)

### Question C

If we hang a current loop from a thread, the magnetic field will exert a torque on the current loop ( $\vec{\tau} = \vec{\mu} \times \vec{B}$ ). This torque will cause the loop to turn until its magnetic dipole moment is aligned with the magnetic field.

Now I ask you: what will be the torque at that moment, and what happens if the current loop is very light?

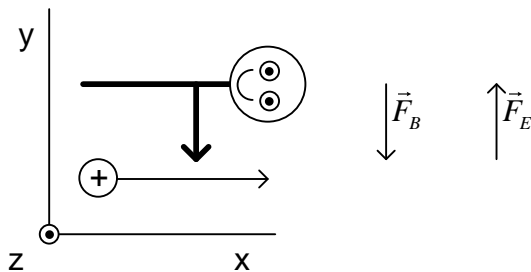
### Question D

$$q_p v_p B = q_\alpha v_\alpha B$$

$$q_\alpha = 2q_p \text{ therefore } v_p = 2v_\alpha$$

Ans: C)

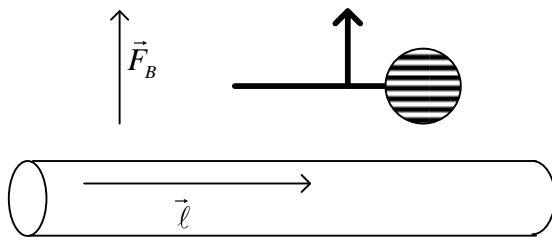
### Question E



$\vec{F}_B$  points down (see ED's arm) so the electric force,  $\vec{F}_E$ , must point up and the electric field must point up as well.

Ans: A)

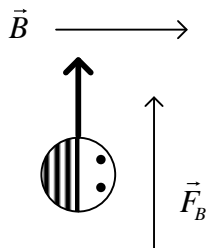
**Question F**



According to the right hand rule as shown above, the magnetic field must point into the page  $\otimes \vec{B}$

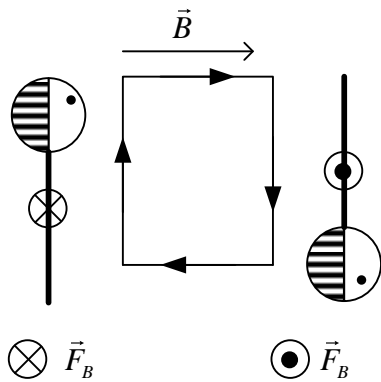
**Question G**

- $\otimes \vec{v}$  negative charge moves down
- $\odot q\vec{v}$  equivalent to positive charge moving up



The force points North

**Question H**



Ans : A

**Question I**

a) The Earth's magnetic field exerts a force on incoming charged particles, deflecting them perpendicular to their velocity. As a result, the particle becomes trapped as it spirals around a magnetic field line. (Particles trapped in the Earth magnetic field form the "van Allen radiation belts")

b) The Earth's magnetic field curve downward and become most dense as they approach the magnetic poles. It is here that the spiralling charged particles are brought closest to the planet; under certain conditions they come low enough to collide with atoms and molecules in the upper atmosphere, producing light.

**Question J**

Yes, if the charge moves parallel to the magnetic field lines there will be no force.

$$F = qvb \sin \theta$$

**Questions K**

No  $\vec{F} = q\vec{v} \times \vec{B}$  the force is always perpendicular to the particle's motion.

**Question L**

Let's do an order of magnitude estimate

$$I \approx 10^5 \text{ A}$$

$$B \approx 10^{-4} \text{ T}$$

So the total force on the 10 m pole (assume  $\perp$  to  $\vec{B}_E$ )

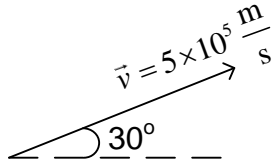
$$F \propto I\ell B \approx (10^5 \text{ A})(10 \text{ m})(10^{-4} \text{ N/Am})$$

$$F \propto I\ell B \approx 100 \text{ N}$$

100 N is the weight of 100 apples, that force is unlikely to bend a flagpole.

**Part B****Question 1**

a)



$$\vec{v} = v \cos 30^\circ \hat{i} + v \sin 30^\circ \hat{j}$$

$$\vec{v} = (4.33 \times 10^5 \hat{i} + 2.50 \times 10^5 \hat{j}) \frac{\text{m}}{\text{s}}$$

$$\vec{F} = q\vec{v} \times \vec{B} = (-1.6 \times 10^{-19}) \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 4.33 \times 10^5 & 2.50 \times 10^5 & 0 \\ 6.00 & -2.00 & 1.00 \end{vmatrix}$$

$$\vec{F} = (-1.6 \times 10^{-19}) \left( (2.50 \times 10^5 \times 1.00) \hat{i} + (-1.00 \times 4.33 \times 10^5) \hat{j} + (4.33 \times 10^5 \times (-2.00) - 6.00 \times 2.50 \times 10^5) \hat{k} \right)$$

$$\vec{F} = (-1.6 \times 10^{-19}) (2.50 \times 10^5 \hat{i} - 4.33 \times 10^5 \hat{j} - 24.3 \times 10^5 \hat{k})$$

$$\vec{F}_B = (-4.00 \hat{i} + 6.93 \hat{j} + 38.9 \hat{k}) \times 10^{-14} \text{ N is the resultant magnetic force}$$

b)  $\vec{F} = q\vec{E}$

We want the electric force to be  $\vec{F}_E = (+4.00 \hat{i} - 6.93 \hat{j} - 38.9 \hat{k}) \times 10^{-14} \text{ N}$  so that  $\vec{F}_E + \vec{F}_B = 0$

$$\vec{E} = \frac{\vec{F}}{q} = \frac{(4.00 \hat{i} - 6.43 \hat{j} - 38.4 \hat{k}) \times 10^{-14}}{-1.60 \times 10^{-19}}$$

$$\vec{E} = (-2.50 \hat{i} + 4.33 \hat{j} + 24.3 \hat{k}) \times 10^5 \frac{\text{N}}{\text{C}}$$

is the electric field we need to make the net force on the electron zero.

**Question 2**

$$\vec{E} = 8.00 \times 10^2 \frac{\text{N}}{\text{C}}$$

$$\vec{B} = 0.800 \text{ T}$$

$$m = 1.16 \times 10^{-26} \text{ kg}$$

“particle is singly charged” therefore:  $q = \pm 1.6 \times 10^{-19} \text{ C}$  (*Can you explain why that is so? Do you think we might ask that on a test?*)

a)

First we find the velocity of the particle in the velocity selector:

$$v = \frac{E}{B} = \frac{8 \times 10^2}{0.8} = 1.00 \times 10^3 \frac{\text{m}}{\text{s}}$$

This is the final velocity of the accelerating stage.

The particle starts from rest so  $v_i = 0 \text{ m/s}$

$$U_i + K_i = U_f + K_f$$

$$U_i - U_f = K_f - K_i$$

$$-\Delta U = \Delta K$$

$$-q\Delta V = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$$

$$\Delta V = \frac{\frac{1}{2} \times 1.16 \times 10^{-26} \times (1 \times 10^3)^2 - 0}{-(-1.6 \times 10^{-19})} = 36.2 \times 10^{-3} \text{ V}$$

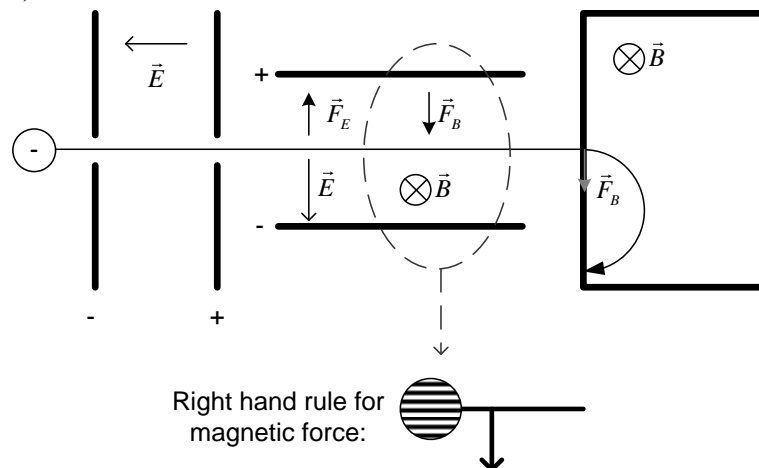
We need to accelerate the particle through a potential difference of 36.2mV

b)

$$r = \frac{mv}{qB} = \frac{1.16 \times 10^{-26} \times 1 \times 10^3}{1.6 \times 10^{-19} \times 0.8} = 9.06 \times 10^{-5} \text{ m}$$

The radius of the circular path followed by the particle once it is inside the chamber is:  $9.06 \times 10^{-5} \text{ m}$

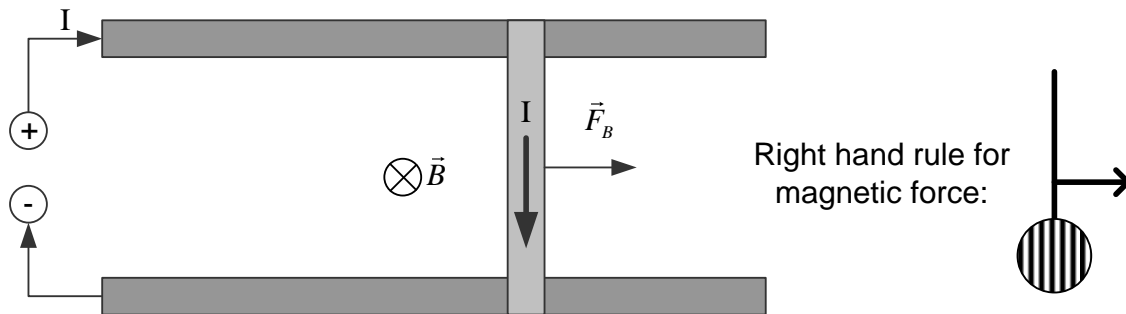
c)



**Question 3**

a)

The magnetic force is to the right (see picture)



b)

*Given :*

$$I = 0.5 \text{ kg}$$

$$\ell = 0.1 \text{ m}$$

$$B = 5.00 \text{ T}$$

$$v_o = 0 \text{ m/s}$$

$$t = 3 \text{ s}$$

*Objective :* a*Strategy :* calculate  $F_B$ , find acceleration and use kinematics to find the final speed

$$F = I\ell B \sin \theta \text{ where } \theta = 90^\circ$$

$$F = 4 \times 0.1 \times 5 = 2.00 \text{ N}$$

$$F = ma$$

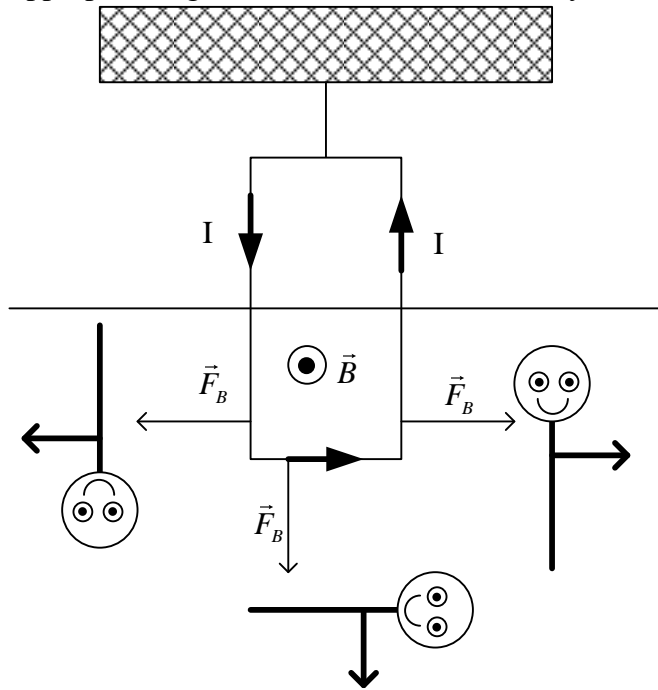
$$a = \frac{F}{m} = \frac{2 \text{ N}}{0.5 \text{ kg}} = 4.00 \frac{\text{m}}{\text{s}^2}$$

$$v = v_o + at = 0 + 4 \times 3 = 12.0 \frac{\text{m}}{\text{s}}$$

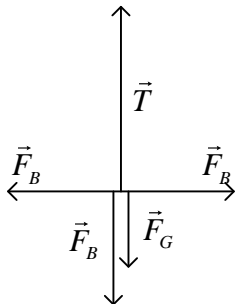
The bar will have a speed of 12 m/s 3 seconds after starting from rest

**Question 4**

Appropriate right hand rules are described by ED's



Free body diagram



List of forces on the y axis :

$$T = ?$$

$$F_G = mg$$

$$F_B = I\ell B \sin \theta$$

By Newton's second law , the sum of the forces should be zero

$$T - F_G - F_B = 0$$

$$T = F_G + F_B = mg + I\ell B \sin \theta = 0.3 \times 9.8 + 3 \times 0.1 \times 2.5 \times \sin 90$$

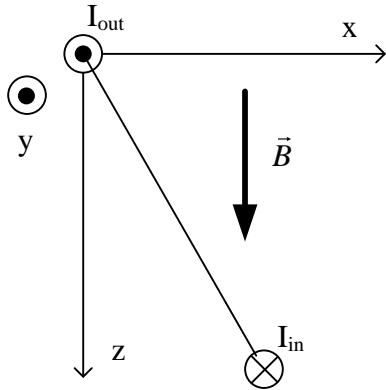
$$T = 3.69 \text{ N}$$

The tension in the string supporting the loop is 3.69 N in positive  $j$  direction.



**Question 5**

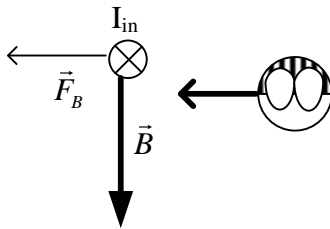
This problem will be easier if we look at the diagram from the positive y-axis:



a)

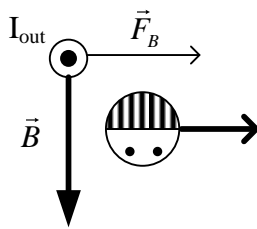
$$F_{ab} = IIB\sin\theta = 5 \times 0.05 \times 0.5 \times \sin 90^\circ$$

$$F_{ab} = 0.125 \text{ N towards the left which we can also write as : } \vec{F}_{ab} = -0.125\hat{i} \text{ N}$$



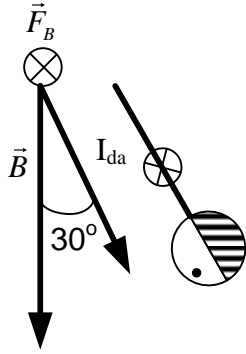
$$F_{cd} = IIB\sin\theta = 5 \times 0.05 \times 0.5 \times \sin 90^\circ$$

$$F_{cd} = 0.125 \text{ N towards the right which we can also write as: } \vec{F}_{cd} = 0.125\hat{i} \text{ N}$$



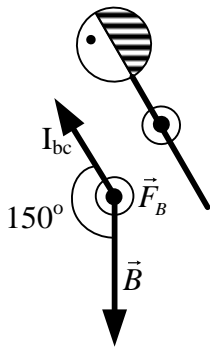
$$F_{da} = IIB\sin\theta = 5 \times 0.05 \times 0.5 \times \sin 30^\circ$$

$$F_{da} = -0.625 \text{ N into the page which we can also write as: } \vec{F}_{da} = -0.0625\hat{j} \text{ N}$$



$$F_{bc} = I l B \sin \theta = 5 \times 0.05 \times 0.5 \times \sin 150^\circ$$

$$F_{bc} = 0.0625 \text{ N out of the page which we can also write as: } \vec{F}_{bc} = 0.0625 \hat{j} \text{ N}$$



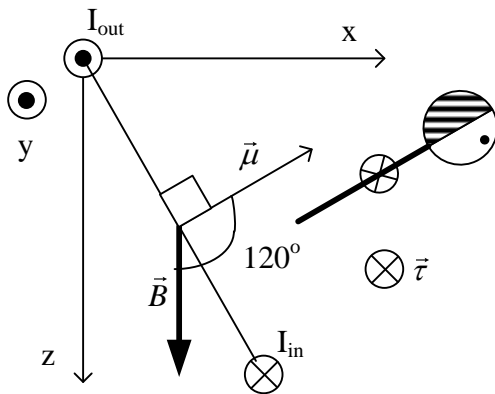
b)

$$\mu = NIA = 1 \times 5 \times 0.05^2 = 0.0125 \text{ Am}^2$$

$$\tau = \mu B \sin \theta$$

$$\tau = 0.125 \times 0.5 \times \sin 120^\circ = 5.41 \times 10^{-3} \text{ Nm}$$

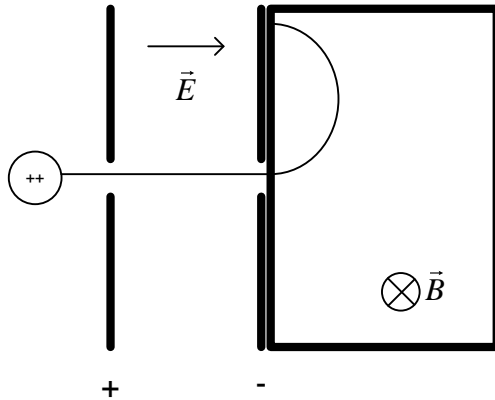
$$\vec{\tau} = -5.41 \times 10^{-3} \hat{j} \text{ Nm}$$



The value of the torque is  $5.41 \times 10^{-3} \text{ Nm}$  pointing in the negative y-direction.

**Question 6**

Given :

« doubly charged positive ion means »  $q = 2 \times 1.6 \times 10^{-19} \text{C}$  $d = 0.2000 \text{ m}$  $E = 5.00 \times 10^4 \text{ V/m}$  $B = 0.5 \text{ T}$  $r = 0.500 \text{ cm}$ 

In the magnetic field, the radius of the particle's trajectory is :  $r = \frac{mv}{qB}$

We know  $r$ ,  $q$ ,  $B$  so we need to find  $v$  to get  $m$

$$\Delta K = -\Delta U$$

$$\Delta K = -q\Delta V$$

$$\frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2 = qEd$$

$$\frac{1}{2}mv_f^2 = qEd$$

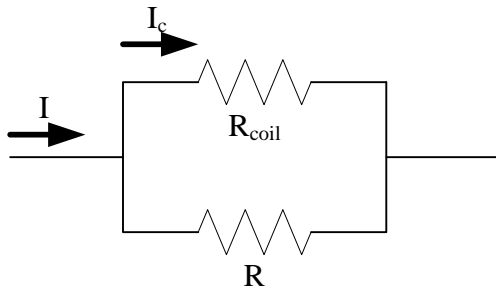
$$v^2 = \frac{2qEd}{m}$$

$$r^2 = \frac{m^2v^2}{q^2B^2}$$

$$r^2 = \frac{m^2 2qEd}{q^2 B^2 m}$$

$$m = \frac{r^2 q^2 B^2}{2qEd} = \frac{(5 \times 10^{-3})^2 \times (2 \times 1.6 \times 10^{-19}) \times 0.5^2}{2 \times 5 \times 10^4 \times 0.2} = 1.00 \times 10^{-28} \text{ kg}$$

So the mass of the particle is  $1.00 \times 10^{-28} \text{ kg}$

**Question 7**

*Strategy:*  $R$  and the coil are in parallel. If we find  $I_c$ , the current in the coil, we will know the voltage across the coil  $V_C$  and therefore across the combination. From  $V$  and  $I$  we will get  $R_{EQ}$ .

$$\tau = 5 \times 10^{-6} \frac{\text{N m}}{\text{deg}} 40 \text{ deg} = 2.00 \times 10^{-4} \text{ Nm}$$

$$\tau = NI_c AB \sin 90$$

$$I_c = \frac{\tau}{NAB} = \frac{2 \times 10^{-4}}{500 \times 0.01^2 \times 7.5 \times 10^{-2}} = 5.33 \times 10^{-2} \text{ A}$$

$$V_C = I_c R_{\text{COIL}} = 5.33 \times 10^{-2} \times 14 = 0.746 \text{ V}$$

$$V_C = IR_{EQ}$$

$$R_{EQ} = \frac{V}{I} = \frac{0.746}{0.500} = 1.49 \Omega$$

The total resistance of the ammeter 1.49 $\Omega$
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