

# **Differential Mortality and Welfare Gains from Social Security Benefit Formula**

Roozbeh Hosseini

Arizona State University

# Social Security

## Old Age and Survivor Insurance (OASI)

- Largest government program in the US
  - collects 3.7% of GDP in tax revenue (2010)
  - pays out 4% of GDP in benefits (2010)
- Major source of income for elderly (40% of all income for 65+)
- It is primarily a retirement pension program, however
  - intragenerational income redistribution is a key part of it
  - and one of the motivations for its existence

## Question

### How Valuable Social Security is as an Income Redistribution Program?

- Social security has a progressive retirement benefit formula
  - it replaces higher fraction of past earnings for low earnings retirees
  
- Social security pays benefits as life annuity
  - it pays more to those who live longer
  - who happen to be high earnings individuals

## Question

### How Valuable Social Security is as an Income Redistribution Program?

- Social security has a progressive retirement benefit formula
  - it replaces higher fraction of past earnings for low earnings retirees
  - ⇒ this is a redistribution from rich to poor within each cohort
- Social security pays benefits as life annuity
  - it pays more to those who live longer
  - who happen to be high earnings individuals

## Question

### How Valuable Social Security is as an Income Redistribution Program?

- Social security has a progressive retirement benefit formula
  - it replaces higher fraction of past earnings for low earnings retirees
  - ⇒ this is a redistribution from rich to poor within each cohort
- Social security pays benefits as life annuity
  - it pays more to those who live longer
  - who happen to be high earnings individuals
  - ⇒ this is a redistribution from poor to rich within each cohort

## Question

### How Valuable Social Security is as an Income Redistribution Program?

- Social security has a progressive retirement benefit formula
  - it replaces higher fraction of past earnings for low earnings retirees
  - ⇒ this is a redistribution from rich to poor within each cohort
- Social security pays benefits as life annuity
  - it pays more to those who live longer
  - who happen to be high earnings individuals
  - ⇒ this is a redistribution from poor to rich within each cohort

### Question:

How much each individual is better off under current system relative to a system that has no redistribution?

# What I do?

- Life cycle OLG model
  - Heterogeneous earnings profiles
  - Differential mortality across earnings profiles
- Calibrate to
  - Current US social security benefit formula
  - Differential mortality rates across lifetime earnings quintiles (estimated by [Cristia \(2007\)](#) using SSA data)
- Counterfactual experiment:

# What I do?

- Life cycle OLG model
  - Heterogeneous earnings profiles
  - Differential mortality across earnings profiles
- Calibrate to
  - Current US social security benefit formula
  - Differential mortality rates across lifetime earnings quintiles (estimated by [Cristia \(2007\)](#) using SSA data)
- Counterfactual experiment:

A pay-as-you-go system with separate balanced budgets for each earnings/mortality group



# What I Find?

## Preview of Results

- If each earnings/mortality group has a separate budget
    - there is no redistribution across these groups, by construction
  - Yet, I find that
    - this yields almost the same replacement ratios as the current system
- ⇒ retirement benefits for each individual is not very different

# What I Find?

## Preview of Results

- If each earnings/mortality group has a separate budget
  - there is no redistribution across these groups, by construction
- Yet, I find that
  - this yields almost the same replacement ratios as the current system
  - ⇒ retirement benefits for each individual is not very different
- ⇒ Welfare is not very different relative to the US system
  - welfare of the very poor is lower by 0.3% of GDP
  - welfare of the very rich is higher by 0.9% of GDP
  - ex ante welfare is lower by 0.004% of GDP

## Related Literature

- Brown et al. (2009), Coronado et al. (2000), Gustman and Steinmeier (2001) use micro simulation to provide various financial measures of redistribution in social security across income groups.
- Brown (2003) uses life cycle model to provide utility based measure of redistribution in a mandatory annuity system across education, sex and race.

# Model

# Model

## Individuals

- Large number of finitely lived individuals born each period
- Individuals are indexed by a parameter  $\theta$ :
  - Drawn from distribution  $\pi(\theta)$
  - Fixed through their lifetime
- Individual of type  $\theta$ 
  - Has – deterministic – earnings ability  $z_j(\theta)$  at age  $j$
  - Has survival rate  $s_{j+1}(\theta)$  at age  $j$

# Model

## Demographics

- Population grows at constant rate  $n$  – for all  $\theta$  types
- There is a maximum age  $J$ :  $s_{J+1}(\theta) = 0 \forall \theta$
- Type  $\theta$  at age  $j$  makes up fraction  $\pi(\theta) \cdot \mu_j(\theta)$  of the population

$$\mu_{j+1}(\theta) = \frac{s_{j+1}(\theta)}{1+n} \cdot \mu_j(\theta)$$

$$\sum_{\theta} \sum_{j=1}^J \pi(\theta) \cdot \mu_j(\theta) = 1$$

$$\sum_{j=1}^J \mu_j(\theta) = 1 \quad \text{for each } \theta$$

## Model

### Preferences

- Individual  $\theta$  has preference over consumption and leisure

$$\sum_{j=1}^J \left( \prod_{i=1}^j s_i(\theta) \right) \beta^{j-1} u(c_j, 1 - h_j)$$

- I assume

$$u(c, 1 - h) = \log(c) + \phi \frac{(1 - h)^{1-\eta}}{1 - \eta}$$

- Everyone retires at age  $J_R$

## Model Technology

- Production technology (variables are per capita and detrended)

$$Y_t = AK_t^\alpha L_t^{1-\alpha}$$

- Output goes to consumption, investment and government purchases

$$C_t + (1+n)(1+g)K_{t+1} + G_t = Y_t + (1-\delta)K_t$$

- Factors are paid their marginal product

$$w_t = (1-\alpha) \cdot \frac{Y_t}{L_t} \text{ and } r_t = \alpha \cdot \frac{Y_t}{K_t} - \delta$$



## Model

### Individual Problem

- Decision problem for individual of type  $\theta$

$$V_j(\theta, a, \bar{e}) = \max_{c \geq 0, a' \geq 0, 1 \geq h \geq 0} u(c, 1 - h) + \beta s_{j+1}(\theta) V_{j+1}(\theta, a', \bar{e}')$$

s.t.

$$(1 + \tau_c)c + a'(1 + g) \leq a(1 + (1 - \tau_k)r) + (1 - \tau_l)wz_j(\theta)h - T_{ss}(wz_j(\theta)h) + B_{ss}(\bar{e}, j) + Tr(\theta)$$

$$\bar{e}' = \begin{cases} \bar{e} + \min \{wz_j(\theta)h, y_{max}\} / 35 & j < 36 \\ \bar{e} & j \geq 36. \end{cases}$$

# Model

## Individual Problem

- Decision problem for individual of type  $\theta$

$$V_j(\theta, a, \bar{e}) = \max_{c \geq 0, a' \geq 0, 1 \geq h \geq 0} u(c, 1 - h) + \beta s_{j+1}(\theta) V_{j+1}(\theta, a', \bar{e}')$$

s.t.

$$(1 + \tau_c)c + a'(1 + g) \leq a(1 + (1 - \tau_k)r) + (1 - \tau_l)wz_j(\theta)h - T_{ss}(wz_j(\theta)h) + B_{ss}(\bar{e}, j) + Tr(\theta)$$

$$\bar{e}' = \begin{cases} \bar{e} + \min \{wz_j(\theta)h, y_{max}\} / 35 & j < 36 \\ \bar{e} & j \geq 36. \end{cases}$$

## Model

### Individual Problem

- Decision problem for individual of type  $\theta$

$$V_j(\theta, a, \bar{e}) = \max_{c \geq 0, a' \geq 0, 1 \geq h \geq 0} u(c, 1 - h) + \beta s_{j+1}(\theta) V_{j+1}(\theta, a', \bar{e}')$$

s.t.

$$(1 + \tau_c)c + a'(1 + g) \leq a(1 + (1 - \tau_k)r) + (1 - \tau_l)wz_j(\theta)h - T_{ss}(wz_j(\theta)h) + B_{ss}(\bar{e}, j) + Tr(\theta)$$

$$\bar{e}' = \begin{cases} \bar{e} + \min \{wz_j(\theta)h, y_{max}\} / 35 & j < 36 \\ \bar{e} & j \geq 36. \end{cases}$$

- $T_{ss}(\cdot)$  and  $B_{ss}(\cdot, j)$  are social security and tax and benefit
- $Tr(\theta)$  is lump-sum transfer

## Model

### Government

- Finances expenditure  $G$

$$G = \tau_c C + \tau_k r \cdot K + \tau_l w \cdot L$$

- Collects and distribute accidental bequest

$$(1 + n) Tr(\theta) = \sum_{j=1}^J \mu_j(\theta) (1 - s_{j+1}(\theta)) (1 + (1 - \tau_k)r) a'_j(\theta)$$

- Runs a pay-as-you-go social security

$$\sum_{\theta} \pi(\theta) \sum_{j=1}^J \mu_j(\theta) [T_{ss}(wz_j(\theta)h_j(\theta)) - B_{ss}(\bar{e}(\theta), j)] = 0$$

# Model

## Social Security Tax and Benefits

- Flat tax rate  $\tau_{SS}$  up to a maximum  $y_{max}$

$$T_{SS}(y) = \begin{cases} \tau_{SS}y & y \leq y_{max} \\ \tau_{SS}y_{max} & y > y_{max} \end{cases}$$

- Benefits are paid after retirement age,  $J_R$

$$B_{SS}(\bar{e}, j) = \begin{cases} 0 & j < J_R \\ \varphi_{SS} b_{US}(\bar{e}) / (1 + g)^{j - J_R} & j \geq J_R. \end{cases}$$

- $b_{US}(\cdot)$  is a nonlinear function of average indexed earning
- $\varphi_{SS}$  is an adjustment parameter to balance the budget

# Calibration

# Calibration

## Earnings Ability Profiles

- Follow Altig et al. (2001), assume 12 income groups

$$\log(z_j(\theta)) = a_0(\theta) + a_1(\theta)j + a_2(\theta)j^2 + a_3(\theta)j^3$$

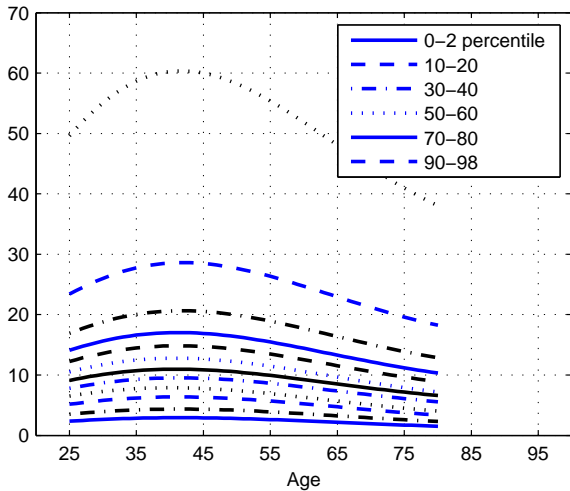
- $\pi(\theta_1) = \pi(\theta_{12}) = 0.02$
- $\pi(\theta_2) = \pi(\theta_{11}) = 0.08$
- $\pi(\theta_3) = \dots = \pi(\theta_{10}) = 0.1$

- Using PSID

1. Run log hourly wages on cubics in age, demographics, fixed effects
2. Use step 1 to generate lifetime-wage profiles
3. Sort according to present value of implied lifetime income
4. Divide into 12 groups – according to above
5. Estimate coefficient  $a_i(\theta)$ 's within each group

# Calibration

## Earnings Ability Profiles





# Calibration

## Demographics

- Use [Bell and Miller \(2005\)](#), male mortality table for cohort of 1940
- Use [Cristia \(2007\)](#) mortality ratios

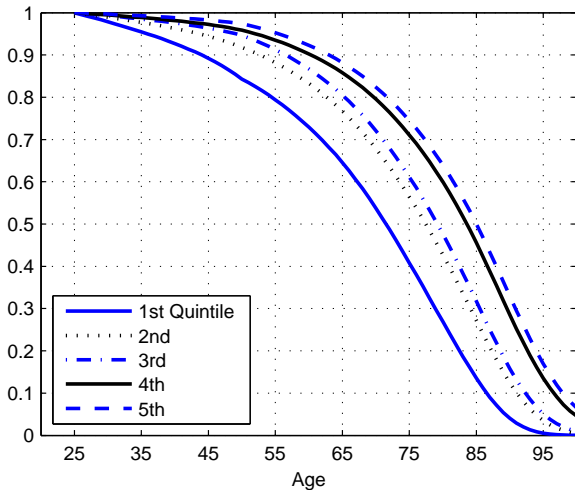
Lifetime Earnings Quintiles	Age Groups		
	35–49	50–64	65–75
Top	0.35	0.61	0.74
Fourth	0.56	0.68	0.94
Third	0.73	0.99	1.08
Second	1.13	1.10	1.14
Bottom	2.25	1.63	1.1

- Construct mortality tables for each earning quintile

mortality for earning quintile<sub>q</sub> = mortality ratio<sub>q</sub> × population mortality

# Calibration

## Unconditional Survival Probabilities for Each Earnings Quintile



# Calibration

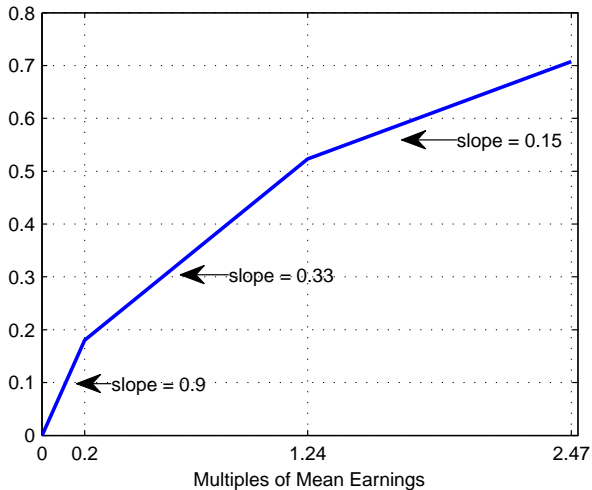
## Social Security Benefit Formula

- Let  $\bar{Y} = w \cdot L$  be the average labor earnings
- Set  $y_{max} = 2.47\bar{Y}$
- Benefit formula

$$b_{US}(\bar{e}) = \begin{cases} 0.9 \times \bar{e} & \bar{e} \leq 0.2\bar{Y} \\ 0.18\bar{Y} + 0.33 \times (\bar{e} - 0.2\bar{Y}) & 0.2\bar{Y} < \bar{e} \leq 1.24\bar{Y} \\ 0.5243\bar{Y} + 0.15 \times (\bar{e} - 1.24\bar{Y}) & \bar{e} > 1.24\bar{Y} \end{cases}$$

# Calibration

## Social Security Benefit Formula



## Calibration Summary

Parameter		Value
$n$		0.011
$J$	ages 25 to 100	76
$\beta$	capital-output ratio of 3	0.9834
$\eta$	labor supply elasticity of 0.4	4.0789
$\phi$	average hours of 0.38	0.3991
$g$		0.0165
$\alpha$		0.36
$\delta$	investment-output ratio of 0.25	0.0557
$A$	wage is normalized to 1	0.8959
$G$	20% of GDP	0.2Y
$\tau_c$	McDaniel (2007)	0.055
$\tau_l = \tau_k$	balance government budget	0.2038
$J_R$	age 65	41
$\tau_{SS}$	social security admin.	0.106
$\varphi_{SS}$	balance social security budget	1.3279

## Quantitative Exercise

## Quantitative Exercise

### A Social Security System with no Redistribution

- Tax function is unchanged

$$T_{NoDist}(y) = T_{ss}(y)$$

## Quantitative Exercise

### A Social Security System with no Redistribution

- Tax function is unchanged

$$T_{NoDist}(y) = T_{ss}(y)$$

- Benefits are constant fraction of average indexed earning

$$B_{NoDist}(\bar{e}, j, \theta) = \begin{cases} 0 & j < J_R \\ \varphi_{NoDist}(\theta) \cdot \bar{e} / (1 + g)^{j - J_R} & j \geq J_R \end{cases}$$



## Quantitative Exercise

### A Social Security System with no Redistribution

- Tax function is unchanged

$$T_{NoDist}(y) = T_{ss}(y)$$

- Benefits are constant fraction of average indexed earning

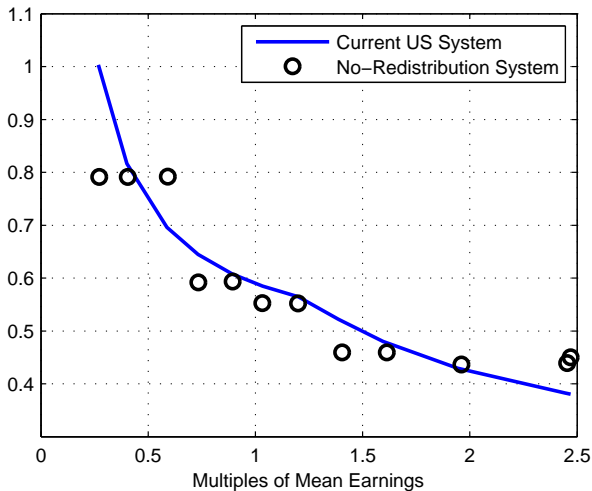
$$B_{NoDist}(\bar{e}, j, \theta) = \begin{cases} 0 & j < J_R \\ \varphi_{NoDist}(\theta) \cdot \bar{e} / (1 + g)^{j - J_R} & j \geq J_R \end{cases}$$

- There is a pay-as-you-go budget for each  $\theta$

$$\sum_{j=1}^J \mu_j(\theta) [T_{NoDist}(wz_j(\theta)h_j(\theta)) - B_{NoDist}(\bar{e}(\theta), j, \theta)] = 0$$

# Replacement Ratios

## US System vs. No-Redistribution System



► what if there is no mortality differential?

# Welfare Comparison

## US System vs. No Redistribution System

- Let  $V^{NoDist}(\theta)$  be welfare of type  $\theta$  under alternative system
- Calculate compensating variations  $x(\theta)$  such that

$$\sum_{j=1}^J \left( \prod_{i=1}^j s_i(\theta) \right) \beta^{j-1} u((1 + x(\theta))c_j^{SS}(\theta), 1 - h_j^{SS}(\theta)) = V^{NoDist}(\theta)$$

- To express a welfare measure as percentage of GDP, plot

$$\frac{\sum_{j=1}^J \mu_j(\theta) x(\theta) c_j(\theta)}{Y}$$

# Welfare Comparison

## US System vs. No Redistribution System

- Let  $V^{NoDist}(\theta)$  be welfare of type  $\theta$  under alternative system
- Calculate compensating variations  $x(\theta)$  such that

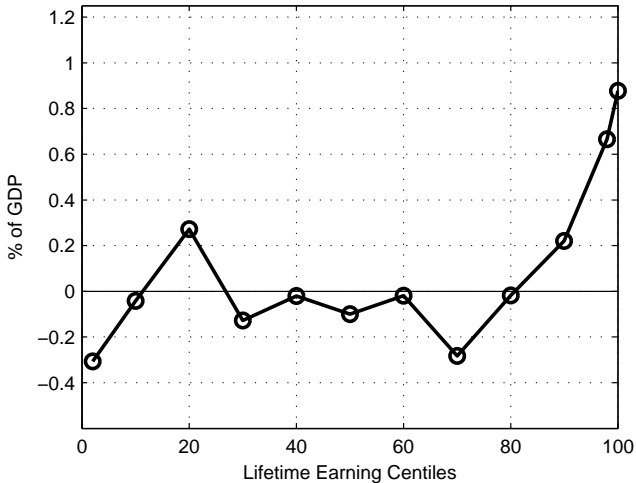
$$\sum_{j=1}^J \left( \prod_{i=1}^j s_i(\theta) \right) \beta^{j-1} u((1 + x(\theta))c_j^{SS}(\theta), 1 - h_j^{SS}(\theta)) = V^{NoDist}(\theta)$$

- To express a welfare measure as percentage of GDP, plot

$$\frac{\sum_{j=1}^J \mu_j(\theta) x(\theta) c_j(\theta)}{Y}$$

# Welfare Comparison

## US System vs. No Redistribution System



▶ what if there is no mortality differential?

# Implications for Aggregates

## US System vs. No Redistribution System

	$Y$	$C$	$H$	$w$	$R$	welfare (% of $Y$ )
Current US	100	55	0.38	16.5	1.051	
No-Redistr.	100.9	55.52	0.384	16.5	1.051	-0.004

$H$  is aggregate hours and  $R$  is return on saving

▶ go to Conclusion

## Alternative Policy 1

### Lump-Sum benefits

- One way to increase progressivity is to pay benefits lump-sum
- This increases replacement ratios for poorer individuals
- At the same time increases labor supply distortions

## Alternative Policy 2

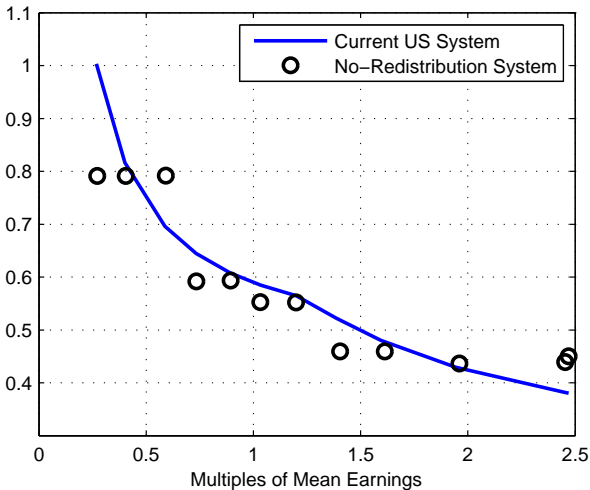
### Start Paying Benefits at 60

- Suppose we pay benefits earlier – say starting at 60yrs old
- This will reduce the effect of differential mortality
- However, the replacement ratios need to be scaled down



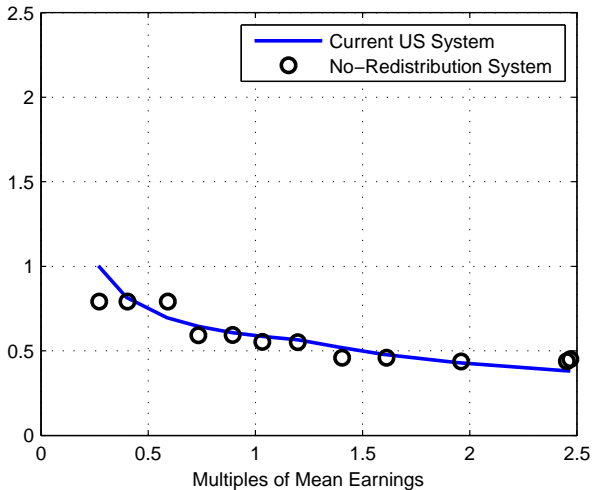
# Replacement Ratios

US System vs. No Redistribution System vs. Lump-Sum vs. Start at 60



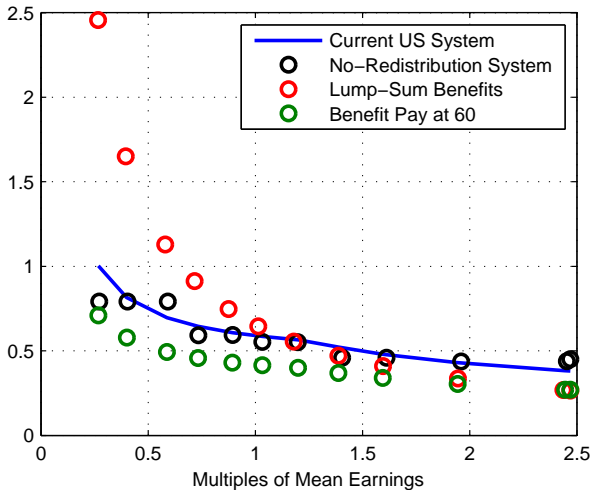
# Replacement Ratios

US System vs. No Redistribution System vs. Lump-Sum vs. Start at 60



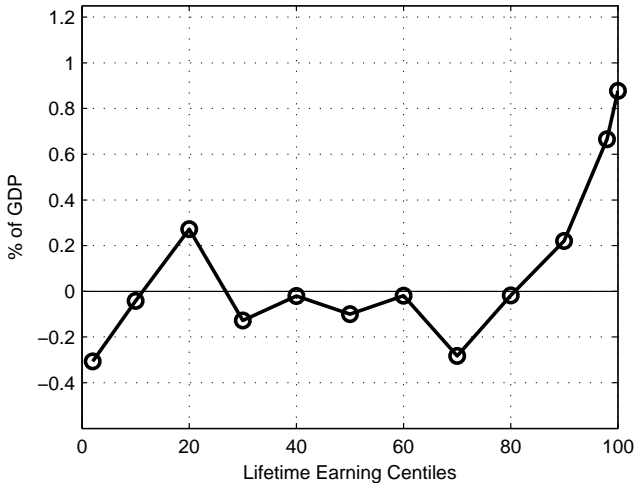
# Replacement Ratios

US System vs. No Redistribution System vs. Lump-Sum vs. Start at 60



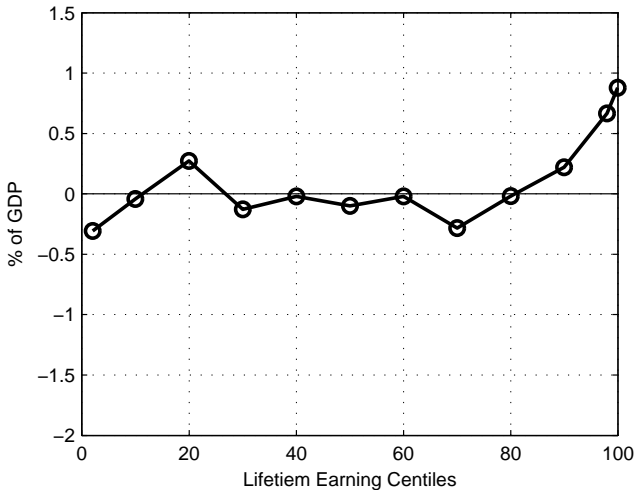
# Welfare Comparison

US System vs. No Redistribution System vs. Lump-Sum vs. Start at 60



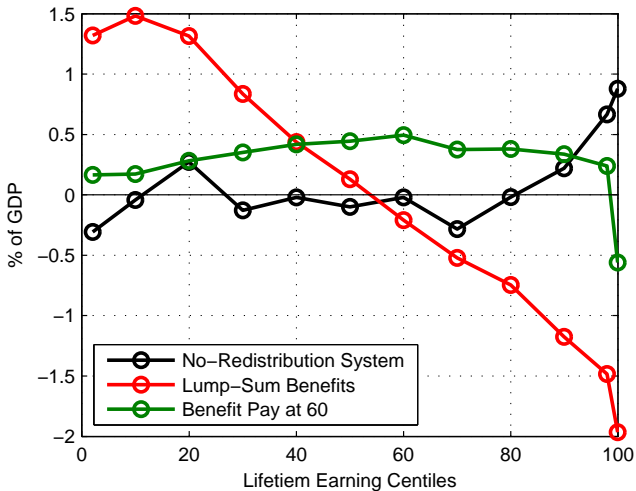
# Welfare Comparison

US System vs. No Redistribution System vs. Lump-Sum vs. Start at 60



# Welfare Comparison

US System vs. No Redistribution System vs. Lump-Sum vs. Start at 60



## Implication for Aggregates

US System vs. No Redistribution System vs. Lump-Sum vs. Start at 60

	$Y$	$C$	$H$	$w$	$R$	welfare (% of $Y$ )
Current US	100	55	0.38	16.5	1.051	
No-Redistr.	100.9	55.52	0.384	16.5	1.051	-0.004
Lump-sum	99	54.23	0.373	16.6	1.050	0.62
Start at 60	100.51	55	0.379	16.6	1.050	0.44

$H$  is aggregate hours and  $R$  is return on saving

## Conclusion

- Progressive benefit formula is one of the key features of US social security system
- One argument against privatization is that progressivity will be lost
- My calculations suggest that this feature of the system is not very valuable



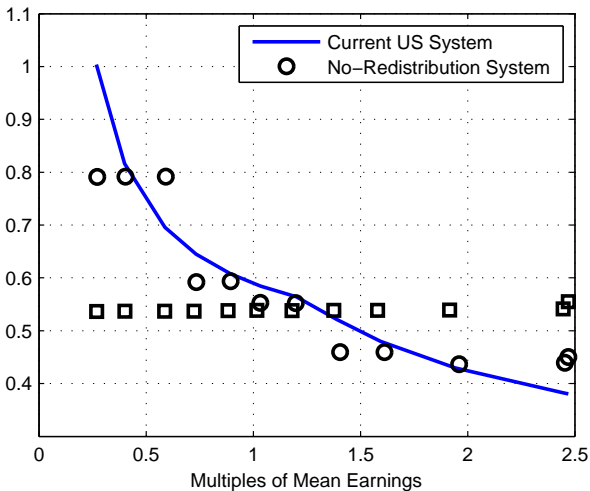
## Conclusion

- Progressive benefit formula is one of the key features of US social security system
- One argument against privatization is that progressivity will be lost
- My calculations suggest that this feature of the system is not very valuable
  
- **To do:** extend the model to include
  - Couples
  - Dependent and survivor benefits

**Back up slides**

# Replacement Ratios without Mortality Heterogeneity

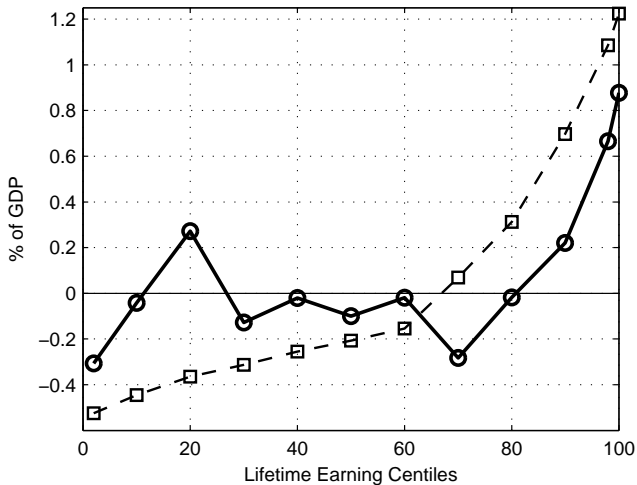
US System vs. No Redistribution System



▶ go back

# Welfare Comparison without Mortality Heterogeneity

## US System vs. No Redistribution System



# References I